

# Background of Component Based Finite Element Method

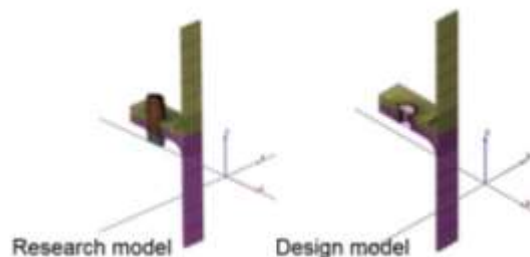


František Wald  
Czech Technical University in Prague

## Motivation

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- Summarise current design of structural connections
- Focus to FEM features
- Explain importance of Validation & Verification



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## List of contents

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- Connection design
  - Models
  - FE analyse
- Validation & verification
- Components modelling
  - Slender plates
  - Bolts
- Connection behaviour
  - Open sections
  - Hollow sections
- Summary



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# Description of behaviour for design by moment-rotation characteristic

## Introduction

Connection design  
Models  
Hollow sections  
Component method  
FE analyse

Validation and verification

Component based FEM  
Slender plates  
Bolted joints

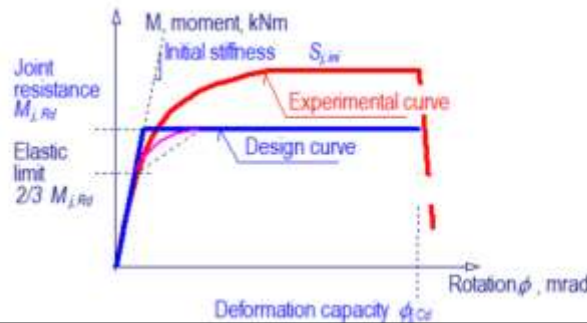
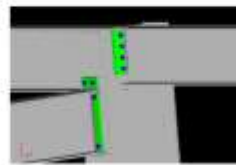
Connection behaviour  
Open sections  
Hollow sections

Summary



Connection exposed to bending

- Rotational stiffness
- Moment resistance
- Rotation capacity



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## Deformation/rotation capacity

### Introduction

Connection design  
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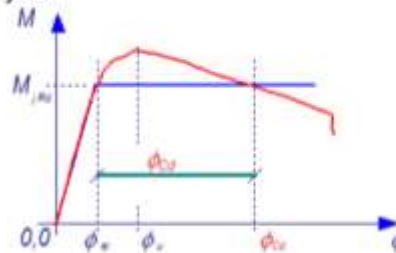
Connection behaviour  
Open sections  
Hollow sections

Summary



### • For safety

- Seismic design
- Plastic global analyses



### • Ductile components

- Plate in bending
- Column web in shear

### • Brittle components

- Bolts, welds

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## Rotation capacity Upper material properties

### Introduction

Connection design  
Models  
Hollow sections  
Component method  
FE analyse

Validation and verification

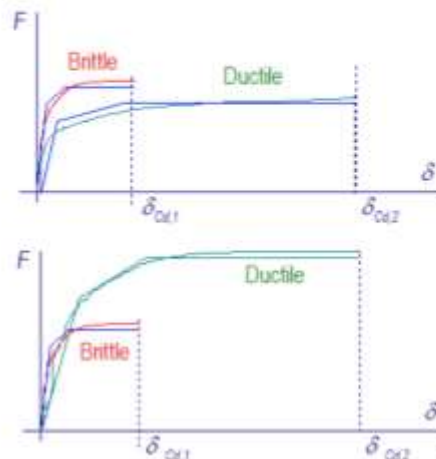
Component based FEM  
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### ○ Question of the Actual yield strength



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# Joint design European standards

- Introduction
- Connection design
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  - Component method
  - FE analysis
- Validation and verification
- Component based
  - FEM
  - Slender plates
  - Bolted joints
- Connection behaviour
  - Open sections
  - Hollow sections
- Summary



- EN1993-1-8, Eurocode 3, **Design of steel structures, Part 1-8, Design of joints**, CEN, Brussels, 2006.
- EN1994-1-1, Eurocode 4, **Design of composite steel and concrete structures, Part 1-1, General rules and rules for buildings**, CEN, 2010.



## Design approaches for structural joints

- Introduction
- Connection design
  - Models
  - Hollow sections
  - Component method
  - FE analysis
- Validation and verification
- Component based
  - FEM
  - Slender plates
  - Bolted joints
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### Models

- Experimental
- Curve fitting
- Analytical
  - Component Method CM
- Finite element analysis
  - Research
  - Design finite element analysis
    - Component based finite element method CBFEM

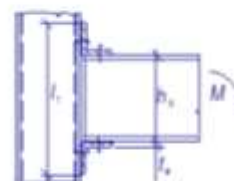
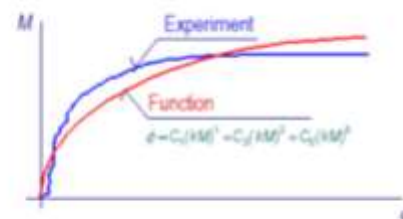
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## Curve fitting model

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- Based on
  - Physical experiments
  - Component method – databases
  - Surrogate models – numerical experiments



- Optimization

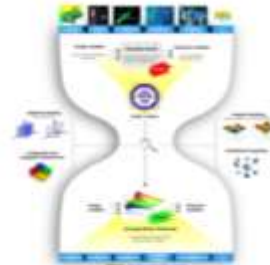
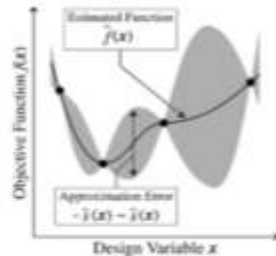
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# Surrogate models

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(Meta models)

- Numerical experiments
- Standardised mathematical procedure



SUMO Delft University 10

## Hollow section joints

- Introduction
- Connection design
  - Models
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- Componentbased FEM
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  - Hollow sections
- Summary

- Design by mixture of
  - Curve fitting
  - Analytical models
- Failure modes
  - CHS, RHS
  - Open and hollow

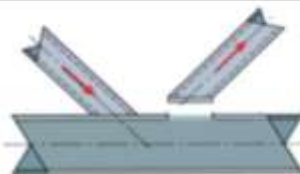


**Mode A:**  
Plastic failure of the chord face

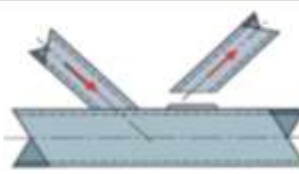


## Hollow section joints

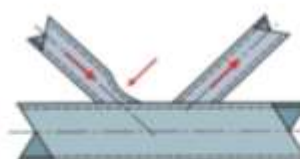
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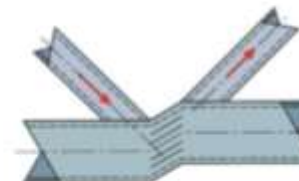
**Mode B:** Punching shear failure of the chord face



**Mode C:** Tension failure of the web member



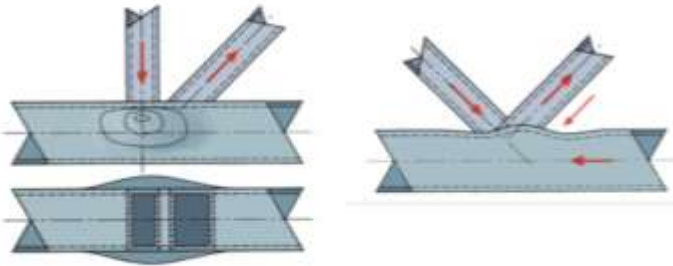
**Mode D:** Local buckling of the web member



**Mode E:** Overall shear failure of the chord

## Hollow section joints

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**Mode F:** Local buckling of the chord walls

**Mode G:** Local buckling of the chord face

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## CIDECT materials

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- Background CIDECT materials
  - ISO/FDIS 14346
  - EN 1993-1-8 Chapter 7
- Uni-planar and multi-planar joints
  - Circular, square or rectangular hollow sections
- +
- Uni-planar joints
  - Combinations of hollow sections with open sections
- Detailed application rules to determine the static resistances of joints in lattice structures

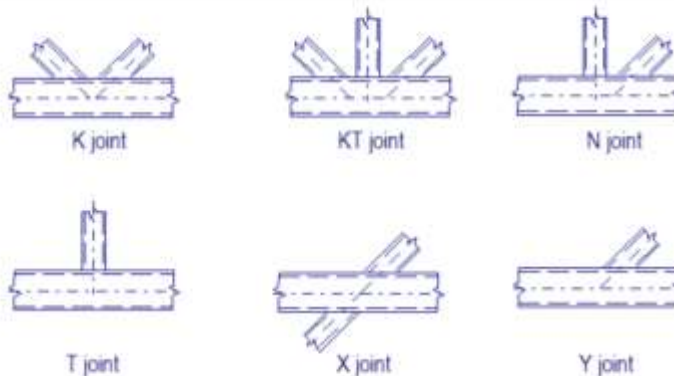


ISO/FDIS 14346: *Static Design Procedure for Welded Hollow Section Joints – Recommendations*, ISO, IIR XV-1439-13, 2012.

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## Geometrical types of basic joints

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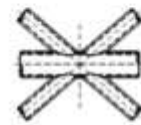
- Class 1 and 2 cross sections
- Limits in geometry

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## Geometrical types of complex joints

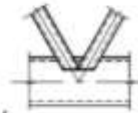
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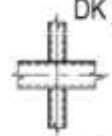
DK joint



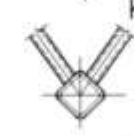
KK joint



TT joint



X joint



XX joint



DY joint

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## Failure modes – chord, shear

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	Rectangular	Circular	Chords of I or H
Chord shear failure			
Punching shear			

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## Failure modes – brace

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 Summary



	Rectangular	Circular	Chords of I or H
Brace failure			
Local buckling			

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## Component based approach for hollow section design

- Introduction
- Connection design
  - Models
  - Hollow sections
  - Component method
  - FE analysis
- Validation and verification
- Component based FEM
  - Slender plates
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- CIDEC project
- 7 failure modes = 7 components
- Defidend lever arm
- The same equations x engineering frendly aproach
- $k_{fa}$  factors transfered to  $b_{eff}$  effective widths

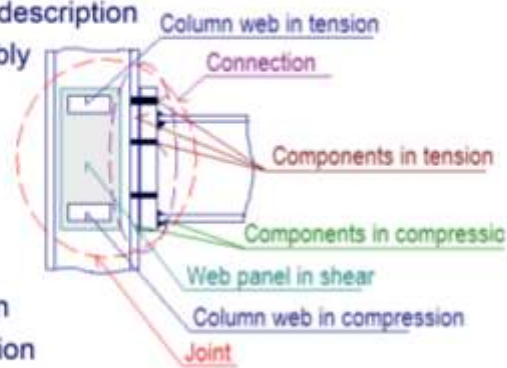
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## Component model Procedure

- Introduction
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- Component based FEM
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- § Decomposition of joint
- § Component description
- § Joint assembly
- § Classification
- § Representation
- § Modelling in analyses

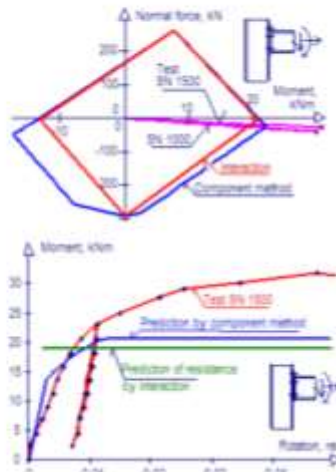


## Component model Prediction accuracy

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- Good accuracy
- M-N Interaction
  - Tests in Prague

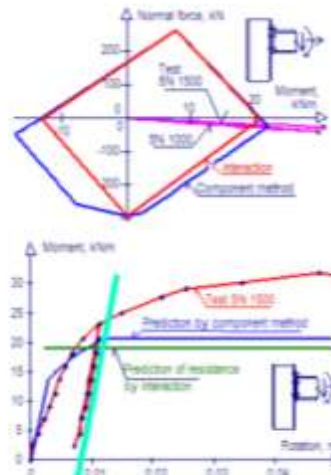


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## Component model Prediction accuracy

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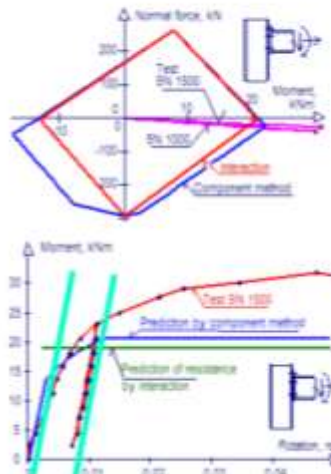


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## Component model Prediction accuracy

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- Good accuracy
- M-N Interaction
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## Component Model Application

- Introduction
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- Summary

- § Design tables
  - § Green book
  - § Blue book
- § Computer programs
- § Simplified hand calculation



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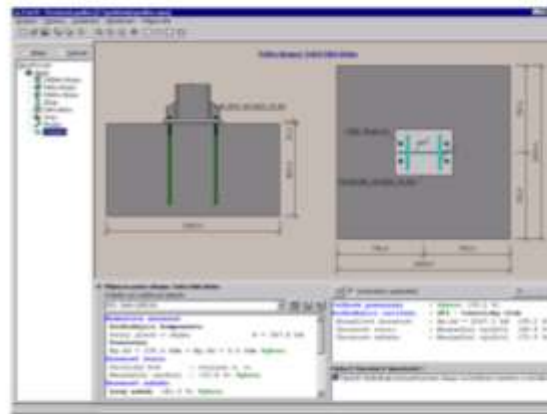


## Component Model Design tools

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- For limited cases



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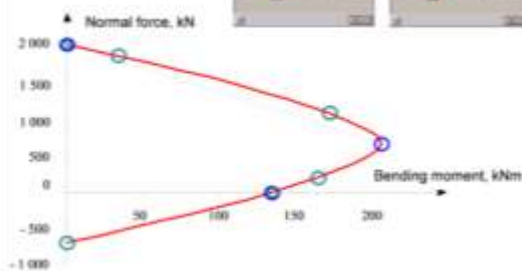
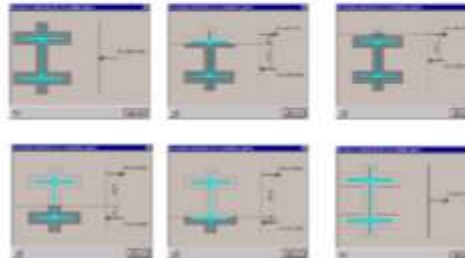
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## Component Model Design tools

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- For limited cases



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## Component model Background references

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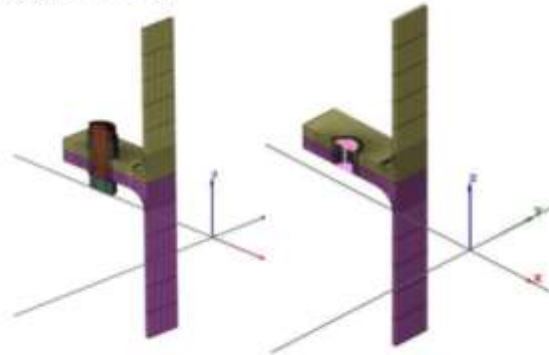


- Zoetemeijer P.: **Summary of the research on bolted beam-to-column connections**, TU-Delft report 26-6-90-2, 1990.
- Zoetemeijer P.: **Summary of the Research on Bolted Beam-to-Column Connections** (period 1978 - 1983), Ref. No. 6-85-M, Steven Laboratory, Delft, 1983.
- Zoetemeijer P.: **Proposal for Standardisation of Extended End Plate Connection based on Test results - Test and Analysis**, Ref. No. 6-83-23, Steven Laboratory, Delft, 1983.
- Jaspart J.P., **Design of structural joints in building frames**, Prog. Struct. Engng Mater., 4, 2002, 18-34.
- Wald F., Sokol Z., Steenhuis M. and Jaspart, J.P., **Component Method for Steel Column Bases**, Heron 53, 2008, 3-20.
- Da Silva Simoes L., **Towards a consistent design approach for steel joints under generalized loading**, JCSR, 64, 2008, 059-1075.
- Beg D., Zupančič E., Vayas I., **On the rotation capacity of moment connections**, JCSR, 60, 3-5, 2004, 601-620.

## Finite Element models of joint

- Introduction
- Connection design
  - Models
  - Hollow sections
  - Component method
  - FE analysis
- Validation and verification
- Componentbased FEM
  - Slender plates
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- Summary

- Research oriented
- Design oriented



Research model

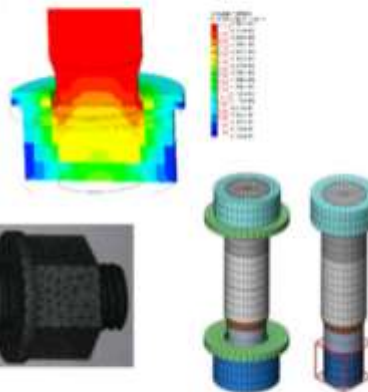
Design model

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## Bolt FEM research models

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- 3D
- Complex
- Material
  - Plasticity criteria
  - Damage model



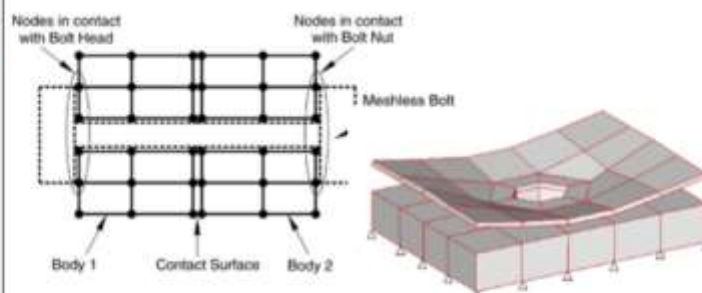
Wu, Z., Zhang, S. and Jiang, S.:  
Simulation of tensile bolts in finite element modeling  
of semi-rigid beam-to-column connections,  
International Journal of Steel Structures, 2012, 12/3, 339-350.

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## Bolts FEM design models

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- Contact model
  - Matricks description



Razavia H., Abolmaalia A., Ghassemieh M., Invisible elastic bolt model concept for finite element analysis of bolted connections, JCSR, 63, 2007, 47-657.

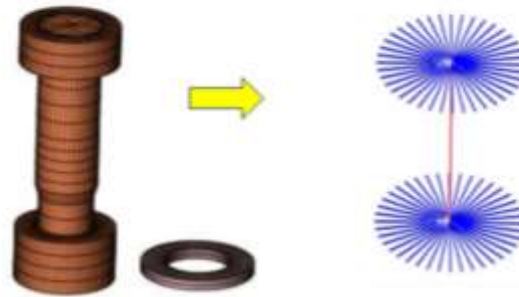
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# FEM modelling of bolts

## Bolts

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### Fan model



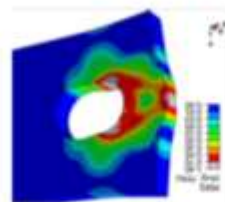
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# Bearing

## FEM modelling

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- von-Mises yield criterion
- Damage models



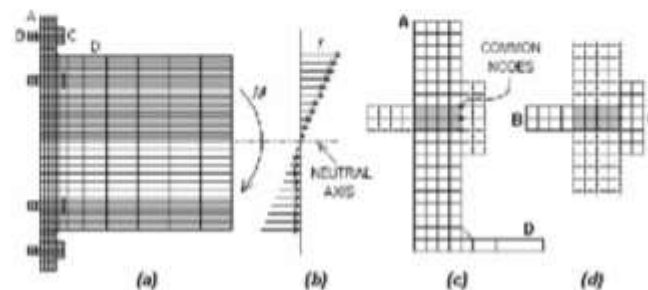
Može P., Beg D., A complete study of bearing stress in single bolt

# Connections

## FE research models

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- N. Krishnamurthy (1978)
  - 3 models
  - 2D model



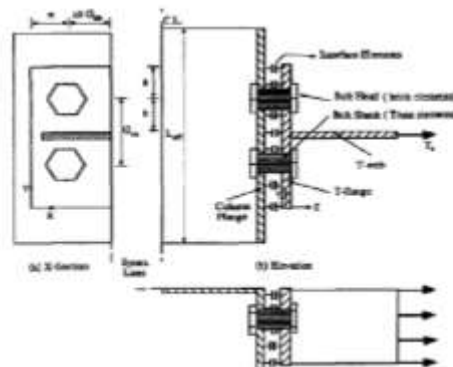
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## Connections FE research models

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- **Bahaari and Sherbourne (1996)**
  - 6 tests, 3D finite element model using ANSYS
  - One of first component based finite element models



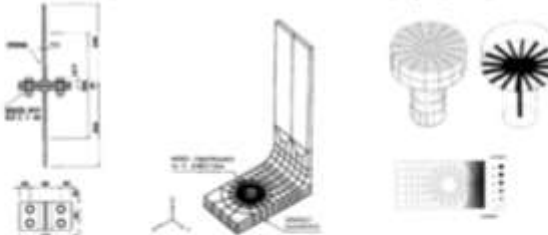
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## Connections FE research models

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- **Bursi and Jaspart (1998)**
  - T-stub and Extended end-plate moment
  - LAGAMINE, a finite element research software
  - Bursi O. S., Jaspart J. P., Benchmarks for Finite Element Modelling of Bolted Steel Connections *Journal of Constructional Steel Research* 43 (1-3), 1997, 17-42



- Used for further validation in COST C1 action
- Viridi K. S. et al, Numerical Simulation of Semi Rigid Connections by the Finite Element Method, Report of Working Group 6 Numerical, Simulation COST C1, Brussels Luxembourg, 1999.

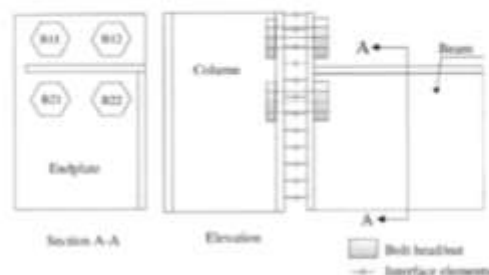
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## Connections FE research models

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- **Bahaari and Sherbourne (1999)**
  - 3D model
  - 4 tests



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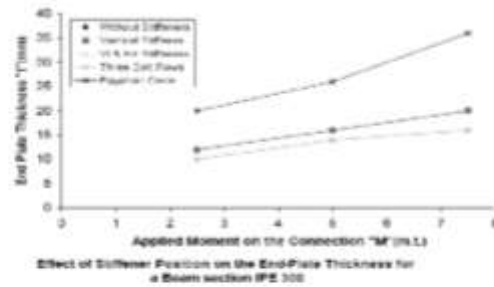


## Connections FE research models

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- N.K. Hassan (2004)
- 2D finite element modeling



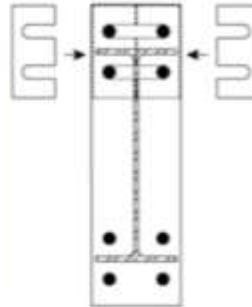
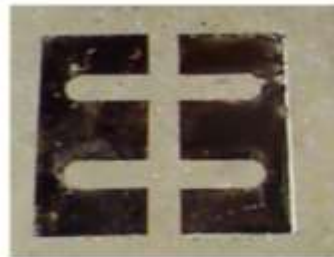
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## Connections FE research models

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- Emmett A. Summer (2003)
- 12 tests, cycling load
- 3D finite element modelling
- Models of finger shims



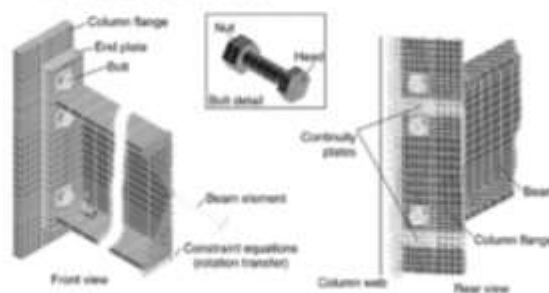
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## Connections FE research models

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- Maggi, Ribeiro (2004)
  - 12 tests
  - four bolts extended unstiffened end-plate moment connections tests
  - ANSYS 3D models



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## Connections FE research models

- Introduction
- Connection design
  - Models
  - Hollow sections
  - Component method
  - FE analysis
- Validation and verification
- Component based FEM
  - Slender plates
  - Bolted joints
- Connection behaviour
  - Open sections
  - Hollow sections
- Summary



- Gang Shi, Yougjiu Shi, Yuanqing Wang, M.A.Bradford (2008)
- 3D finite element modeling
- 6 experiments



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## Validation and verification procedures

- Introduction
- Connection design
  - Models
  - Hollow sections
  - Component method
  - FE analysis
- Validation and verification
- Component based FEM
  - Slender plates
  - Bolted joints
- Connection behaviour
  - Open sections
  - Hollow sections
- Summary



- Well developed in FEM theory
- To check the physical accuracy
- To check the proper use
- To check the asked design level



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## Definitions of Verification & Validation

- Introduction
- Connection design
  - Models
  - Hollow sections
  - Component method
  - FE analysis
- Validation and verification
- Component based FEM
  - Slender plates
  - Bolted joints
- Connection behaviour
  - Open sections
  - Hollow sections
- Summary



### Validation

compares the numerical solution with the experimental data.

**Validation** can be practically split into three tasks:

- to detect and separate the model's significant discrepancies,
- to remove and reduce removable and unavoidable errors,
- to evaluate uncertainties in the results.

### Verification

uses comparison of computational solutions with highly accurate (analytical or numerical)

**Verification** is supposed to deliver evidence that mathematical models are properly implemented and that the numerical solution is correct with respect to the mathematical model.

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Introduction

Connection design

Models

Hollow sections

Component method

FE analyse

**Validation and verification**

Component based FEM

Slender plates

Boxed joints

Connection behaviour

Open sections

Hollow sections

Summary

## Definitions of Verification & Validation

**ISO/FDIS 16730**  
Fire safety engineering - Assessment, verification and validation of calculation methods, Geneva, 2008.

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Introduction

Connection design

Models

Hollow sections

Component method

FE analyse

**Validation and verification**

Component based FEM

Slender plates

Boxed joints

Connection behaviour

Open sections

Hollow sections

Summary

## General Aspects of Modeling

Kikamiawaki L. (2009) On practical problems with verification and validation of computational models. Archives of Civil Engineering, LV, 3, 323-346.

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Introduction

Connection design

Models

Hollow sections

Component method

FE analyse

**Validation and verification**

Component based FEM

Slender plates

Boxed joints

Connection behaviour

Open sections

Hollow sections

Summary

## Spectacular example of a software bug

**F-22 Squadron Shot Down by the International Date Line (2007)**

**Maj. Gen. Don Sheppard (ret.):**

"...At the international date line, whoops, all systems dumped and when I say all systems, I mean all systems, their navigation, part of their communications, their fuel systems.

.....

It was a computer glitch in the millions of lines of code, somebody made an error in a couple lines of the code and everything goes."

<http://www.defenseindustrydaily.com>

\$120 million F-22 Raptor

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# Famous warning Sinking offshore platform Sleipner A

- Introduction
- Connection design
  - Models
  - Hollow sections
  - Component method
  - FE analyse
- Validation and verification
- Componentbased FEM
  - Slender plates
  - Boxed joints
- Connection behaviour
  - Open sections
  - Hollow sections
- Summary

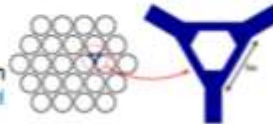
- Failure in a cell wall
- Serious crack and leakage
- Pumps were not able to cope with
- Combination of a serious error in FEM
- Insufficient anchorage of the reinforcement in a critical zone



- Inaccurate finite element approximation
- **Linear elastic model of the tricell NASTRAN**
- Shear stresses underestimated by 47 %
- Certain concrete walls not thick enough

- Total economic loss of about \$700 million

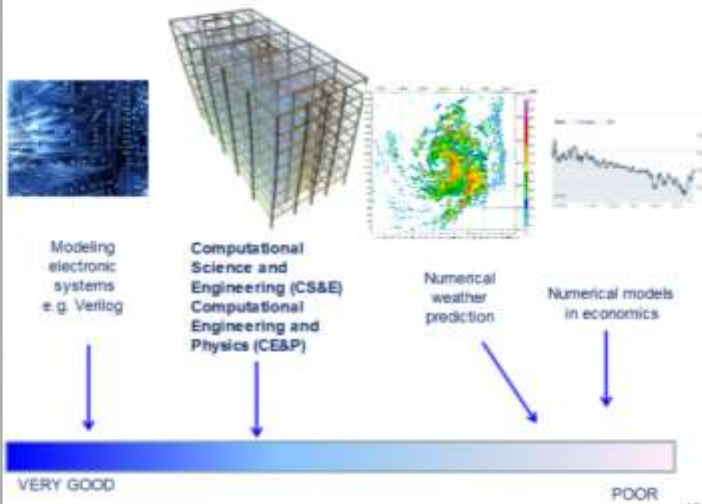
<http://www.uma.umh.edu/~arnold/disasters/sleipner.html>



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## What are the predictive capabilities of our computer simulations?

- Introduction
- Connection design
  - Models
  - Hollow sections
  - Component method
  - FE analyse
- Validation and verification
- Componentbased FEM
  - Slender plates
  - Boxed joints
- Connection behaviour
  - Open sections
  - Hollow sections
- Summary

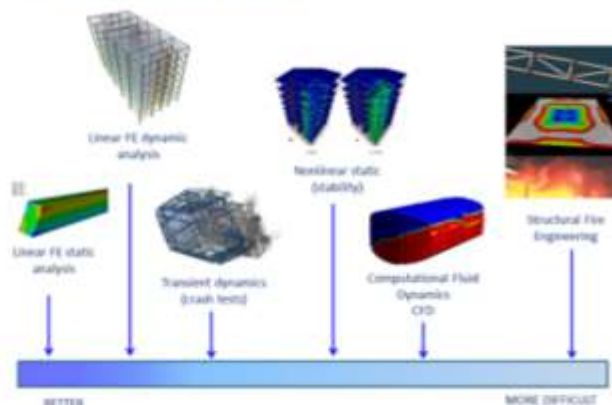


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## Computational Science and Engineering (CS&E)

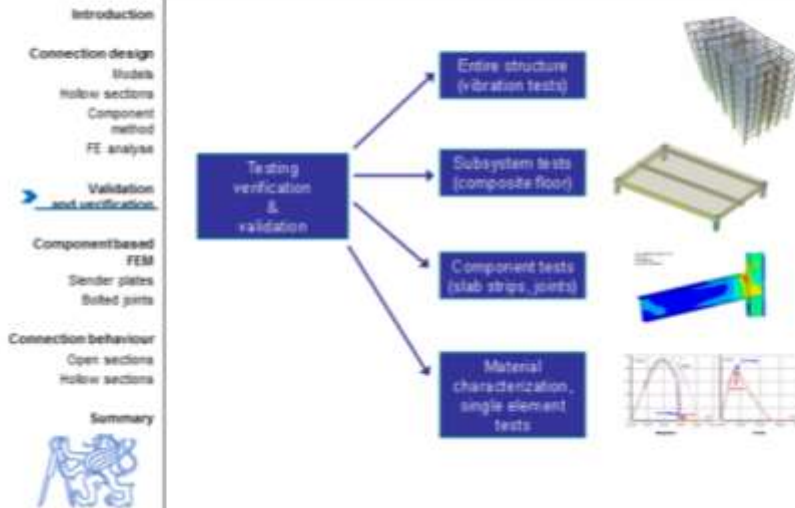
- Introduction
- Connection design
  - Models
  - Hollow sections
  - Component method
  - FE analyse
- Validation and verification
- Componentbased FEM
  - Slender plates
  - Boxed joints
- Connection behaviour
  - Open sections
  - Hollow sections
- Summary

### Predictive Capabilities



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## Hierarchy validation and verification



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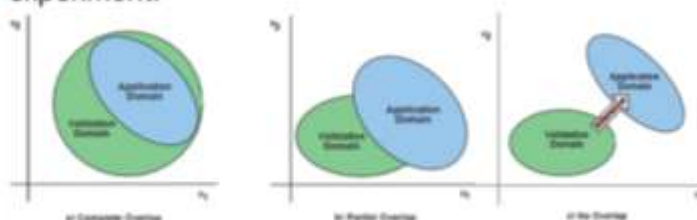
## System response quantity SRQ

- Introduction
- Connection design  
Models  
Hollow sections  
Component method  
FE analysis
- Validation and verification
- Component based FEM  
Slender plates  
Bolted joints
- Connection behaviour  
Open sections  
Hollow sections
- Summary
- Validation is based on the comparison between computational results and experimental data
  - An experiment can provide much less information than the calculation
  - Selection of the system response quantity (SRQ) is limited by the experiment output

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## Validation domains

- Introduction
- Connection design  
Models  
Hollow sections  
Component method  
FE analysis
- Validation and verification
- Component based FEM  
Slender plates  
Bolted joints
- Connection behaviour  
Open sections  
Hollow sections
- Summary
- Application domain**  
defines the intended boundaries for the predictive capability of the computational model
- Validation domain**  
characterizes the representation capabilities of the experiment.



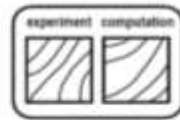
W.G. Ockers, T.G. Thureau, C. Hirsch, Verification, validation, and predictive capability in computational engineering and physics, Appl. Mech. Rev. 57 (3), 343–384, 2004

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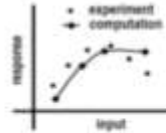


## Validation metrics

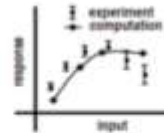
Introduction
Connection design
Models
Hollow sections
Component method
FE analyse
<b>Validation and verification</b>
Componentbased FEM
Slender plates
Bolted joints
Connection behaviour
Open sections
Hollow sections
Summary



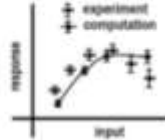
(a) Viewgraph Norm



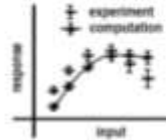
(b) Deterministic



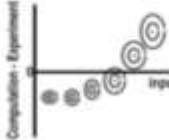
(c) Experimental Uncertainty



(d) Numerical Error



(e) Nondeterministic Computation



(f) Quantitative Comparison

W.L. Oberkampf, T.G. Trucano, C. Hirsch, Verification, validation, and predictive capability in computation engineering and physics, Appl. Mech. Rev. 57 (3), 345-384, 2004.

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## Evaluation of Mechanical Structural Response

Introduction
Connection design
Models
Hollow sections
Component method
FE analyse
<b>Validation and verification</b>
Componentbased FEM
Slender plates
Bolted joints
Connection behaviour
Open sections
Hollow sections
Summary



- **Local quantities**
  - Stresses
  - Internal forces
  - Larger uncertainties especially
- **Global quantities**
  - Deflection
  - Whole (or a large part) of structure
  - Boundary condition

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## Verification - Mesh density study

Introduction
Connection design
Models
Hollow sections
Component method
FE analyse
<b>Validation and verification</b>
Componentbased FEM
Slender plates
Bolted joints
Connection behaviour
Open sections
Hollow sections
Summary



- Discretization error  $E = f_h - f_{exact} = Ch^p + H.O.T.$

- Order of convergence  $p = \frac{\ln(f_h - f_k)}{\ln(r)}$
- Estimate of the asymptotic solution

$$f_h \approx f_1 + \frac{f_1 - f_2}{r^p - 1}$$

- $E_1$  is the estimator of the relative error

$$E_1 = \frac{f_1 - f_2}{f_1}, \quad \varepsilon = \frac{f_1 - f_2}{f_1}$$

- **Grid Convergence Index** - GCI procedure (Richardson extrapolation)

$$GCI = \frac{E_1}{r^p - 1} 100\%$$

Roache P.J., Verification and validation in computational science and engineering, Computing in Science Engineering, Hermosa pub., 1988, 8-9.

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# Verification and Validation of Computer Simulations

Introduction

Connection design

Models

Hollow sections

Component

method

FE analyse

Validation and verification

Componentbased

FEM

Slender plates

Noted joints

Connection behaviour

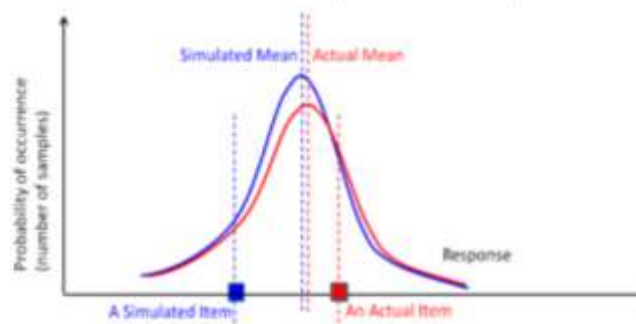
Open sections

Hollow sections

Summary



## FE model well replicates the experiment



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# Verification and Validation of Computer Simulations

Introduction

Connection design

Models

Hollow sections

Component

method

FE analyse

Validation and verification

Componentbased

FEM

Slender plates

Noted joints

Connection behaviour

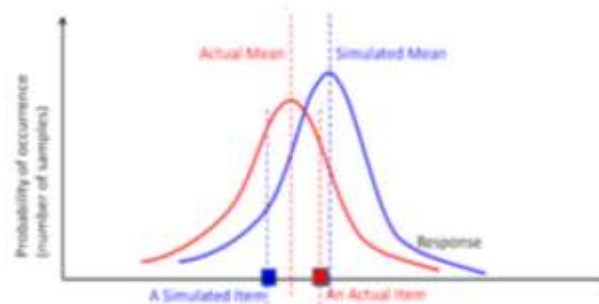
Open sections

Hollow sections

Summary



## Effect of calibration



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# Databases of benchmark problems

Introduction

Connection design

Models

Hollow sections

Component

method

FE analyse

Validation and verification

Componentbased

FEM

Slender plates

Noted joints

Connection behaviour

Open sections

Hollow sections

Summary



## • National Agency for Finite Element Methods and Standards (NAFEMS) [www.nafems.org](http://www.nafems.org)

- ~ 280 verification benchmarks

## • ABAQUS Benchmarks Manual

- 264 (93-NAFEMS, 15-thermal analysis) Verification Manual, Example Problems Manual

## • ANSYS® - around 250 problems

## • Fire engineering

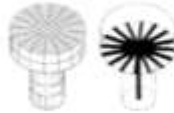
- Standardised ISO/FDIS 16730  
Fire safety engineering — Assessment, verification and validation of calculation methods, Geneva, 2008.
- DIN EN 1991-1-2

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## Validation of research model of T stub

Introduction
Connection design
Models
Hollow sections
Component method
FE analyse
<b>Validation and verification</b>
Component based FEM
Slender plates
Bolted joints
Connection behaviour
Open sections
Hollow sections
Summary

- Modern history
  - 1997
    - Bursi O. S., Jaspart J. P., Benchmarks for Finite Element Modelling of Bolted Steel Connections, *Journal of Constructional Steel Research*, 43 (1-3), 1997, 17-42.
  - 1999
    - Viridi K. S. et al, *Numerical Simulation of Semi Rigid Connections by the Finite Element Method*, Report of Working Group 6 Numerical, Simulation COST C1, Brussels Luxembourg, 1999.



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## Hierarchy of benchmark studies for structural steel joints

Introduction
Connection design
Models
Hollow sections
Component method
FE analyse
<b>Validation and verification</b>
Component based FEM
Slender plates
Bolted joints
Connection behaviour
Open sections
Hollow sections
Summary

- **Welded joints**
  - In shear
  - In bending
  - Long joint
  - Flexible plate
- **Bolted connections**
  - T-stub in tension
  - Splices in shear
  - Generally loaded end plate
- **Slender plate in compression**
  - Triangular haunch
  - Stiffener of column web
  - Plate in compression between bolts
- **Hollow section joints**
  - CHS, RHS members
  - Hollow and open sections
- **Column bases**
  - T stub in compression and in tension
  - Generally loaded base plate

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## Verification and Benchmark cases

Introduction
Connection design
Models
Hollow sections
Component method
FE analyse
<b>Validation and verification</b>
Component based FEM
Slender plates
Bolted joints
Connection behaviour
Open sections
Hollow sections
Summary

### Chapters

- Description
- Component method
- CBFEM
- Force-deformation curve
- Global behaviour
- Verification of resistance
- Global verification
- Initial stiffness, Resistance, Deformation capacity
- Benchmark case



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# Component based FEM

- Introduction
- Connection design
  - Models
  - Hollow sections
  - Component method
  - FE analyse
- Validation and verification
- Component based FEM
  - Slender plates
  - Bolted joints
- Connection behaviour
  - Open sections
  - Hollow sections
- Summary

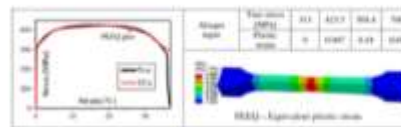
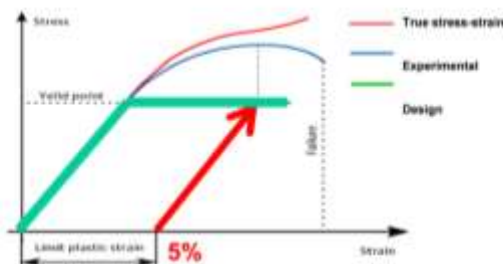
- Joint analyses by FEM
  - Design material model
- Component behaviour
  - Connectors
    - Bolts
      - In tension
      - In shear
    - Welds
    - Anchor bolts
  - Slender plates
  - Concrete block

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## Material for FE design model

- Introduction
- Connection design
  - Models
  - Hollow sections
  - Component method
  - FE analyse
- Validation and verification
- Component based FEM
  - Slender plates
  - Bolted joints
- Connection behaviour
  - Open sections
  - Hollow sections
- Summary

- Bilinear ideal elastic-plastic model



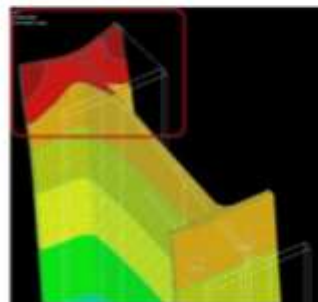
Mohd P., Beg D., A complete study of bearing stress in single bolt connections, JCSR, 9 5 (2014) 126-140

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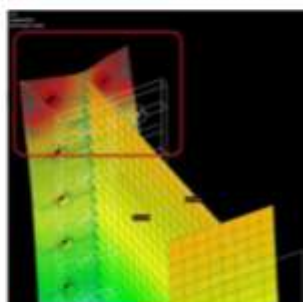
## Plate modelling

- Introduction
- Connection design
  - Models
  - Hollow sections
  - Component method
  - FE analyse
- Validation and verification
- Component based FEM
  - Slender plates
  - Bolted joints
- Connection behaviour
  - Open sections
  - Hollow sections
- Summary

### 3D – bricks



### 2D elements - shells



- Shells for design
  - 8 degree of freedom elements
  - 4 nodes (degrades to 3)
  - Allowing plastification, membrane effects, bifurcation

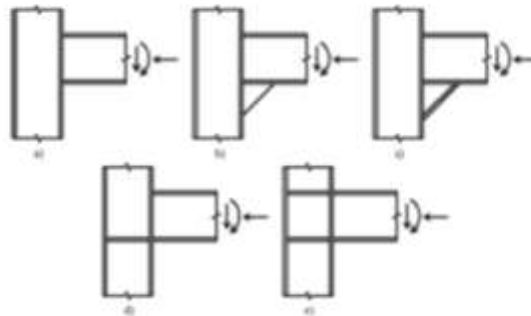
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## Design model Slender plate in compression

Introduction  
Connection design  
Models  
Hollow sections  
Component method  
FE analyse  
Validation and verification  
Component based FEM  
→ Slender plates  
Bolted joints  
Connection behaviour  
Open sections  
Hollow sections  
Summary



- Column web
- Stiffeners



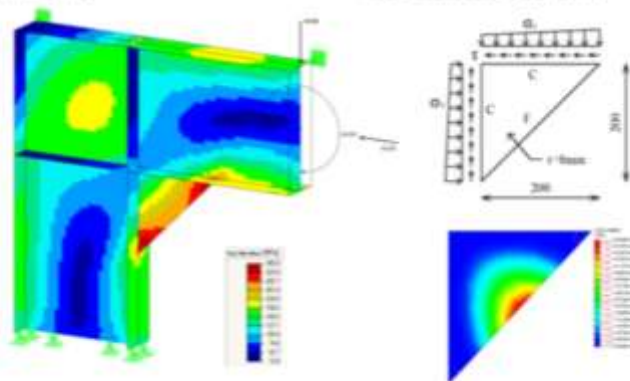
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## FE research model on T triangular stiffener

Introduction  
Connection design  
Models  
Hollow sections  
Component method  
FE analyse  
Validation and verification  
Component based FEM  
→ Slender plates  
Bolted joints  
Connection behaviour  
Open sections  
Hollow sections  
Summary



- Von-Mises stress distribution for beam-to-column joint  
In frame at a separate element



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## Research FEM

Introduction  
Connection design  
Models  
Hollow sections  
Component method  
FE analyse  
Validation and verification  
Component based FEM  
→ Slender plates  
Bolted joints  
Connection behaviour  
Open sections  
Hollow sections  
Summary



- Shell elements, true-stress true strain material model, mesh sensitivity
- Geometrical and material nonlinear model with imperfections (GMNIA)
- Imperfections based on 1<sup>st</sup> buckling mode
- Experiments – literature, own
- Code RFEM



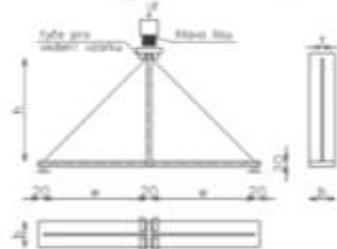
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## Experimental research

Introduction  
 Connection design  
 Models  
 Hollow sections  
 Component method  
 FE analyse  
 Validation and verification  
 Component based FEM  
 → **Slender plates**  
 Bolted joints  
 Connection behaviour  
 Open sections  
 Hollow sections  
 Summary

- Material tests
- Flanges
  - 3x free edge, 3x partial stiffener, 3x fully stiffening
- Variation of
  - Stiffener thickness  $t$
  - Haunch geometry  $h$  and  $w$
  - Flange thickness  $t_f$  and width  $b_f$



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## Supports and loading

Introduction  
 Connection design  
 Models  
 Hollow sections  
 Component method  
 FE analyse  
 Validation and verification  
 Component based FEM  
 → **Slender plates**  
 Bolted joints  
 Connection behaviour  
 Open sections  
 Hollow sections  
 Summary

- Hinges and compression
- Strain gauges LY11-6/120 a XY11-6/120
- Deflectometers
- Loading by steps till collapse



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## Stiffener with free edge

Introduction  
 Connection design  
 Models  
 Hollow sections  
 Component method  
 FE analyse  
 Validation and verification  
 Component based FEM  
 → **Slender plates**  
 Bolted joints  
 Connection behaviour  
 Open sections  
 Hollow sections  
 Summary

$h = 400 \text{ mm}$ ,  $w = 200 \text{ mm}$ ,  $t = 6 \text{ mm}$



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## Stiffener with free edge

Introduction

Connection design

Models

Hollow sections

Component

method

FE analyse

Validation  
and verification

Component based

FEM

→ Slender plates

Botled joints

Connection behaviour

Open sections

Hollow sections

Summary



$h = w = 400 \text{ mm}$ ,  $t = 4 \text{ mm}$  and  $t = 6 \text{ mm}$



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## Stiffener with partial stiffened edge

Introduction

Connection design

Models

Hollow sections

Component

method

FE analyse

Validation  
and verification

Component based

FEM

→ Slender plates

Botled joints

Connection behaviour

Open sections

Hollow sections

Summary



$h = w = 400 \text{ mm}$ ,  $t = 6 \text{ mm}$ ,  $t_f = 6 \text{ mm}$ ,  $b_f = 60 \text{ mm}$



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## Stiffener with partial stiffened edge

Introduction

Connection design

Models

Hollow sections

Component

method

FE analyse

Validation  
and verification

Component based

FEM

→ Slender plates

Botled joints

Connection behaviour

Open sections

Hollow sections

Summary



$h = w = 400 \text{ mm}$ ,  $t = 6 \text{ mm}$ ,  $t_f = 12 \text{ mm}$ ,  $b_f = 120 \text{ mm}$



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## Stiffener with partial stiffened edge

- Introduction
- Connection design
  - Models
  - Hollow sections
  - Component method
  - FE analyse
- Validation and verification
- Componentbased FEM
  - Slender plates
  - Bolted joints
- Connection behaviour
  - Open sections
  - Hollow sections
- Summary

$h = w = 400 \text{ mm}$ ,  $t = 4 \text{ mm}$ ,  $t_f = 12 \text{ mm}$ ,  $b_f = 120 \text{ mm}$



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- Introduction
- Connection design
  - Models
  - Hollow sections
  - Component method
  - FE analyse
- Validation and verification
- Componentbased FEM
  - Slender plates
  - Bolted joints
- Connection behaviour
  - Open sections
  - Hollow sections
- Summary

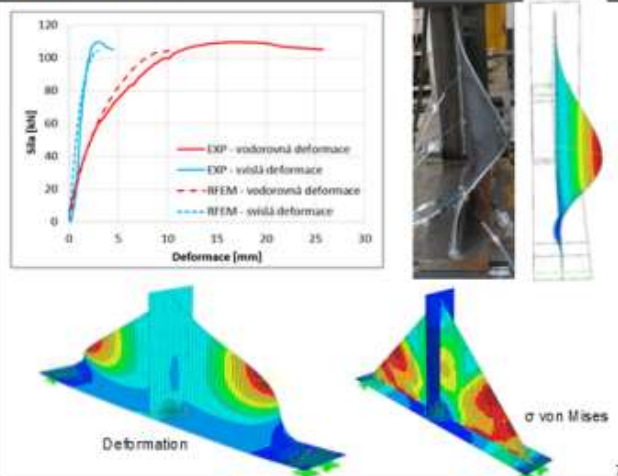
- Validation on force-deformation curve  $F-\delta$  for resistance
- Vertical deformation at centre
- Vertical deformation at max. amplitude



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## Validation of research model Free edge

- Introduction
- Connection design
  - Models
  - Hollow sections
  - Component method
  - FE analyse
- Validation and verification
- Componentbased FEM
  - Slender plates
  - Bolted joints
- Connection behaviour
  - Open sections
  - Hollow sections
- Summary



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## Validation of research model Partial stiffened edge

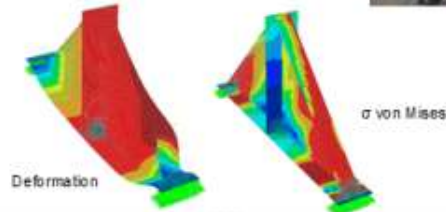
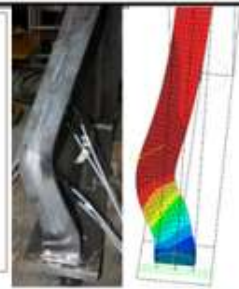
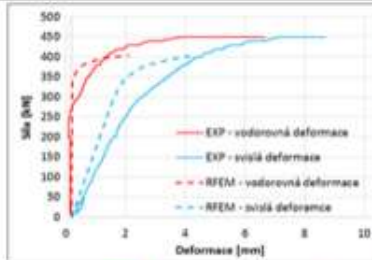
Introduction  
Connection design  
Models  
Hollow sections  
Component method  
FE analyse

Validation and verification

Componentbased FEM  
Slender plates  
Bolted joints

Connection behaviour  
Open sections  
Hollow sections

Summary



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## Validation of FE research model on T triangular stiffener tests

Introduction  
Connection design  
Models  
Hollow sections  
Component method  
FE analyse

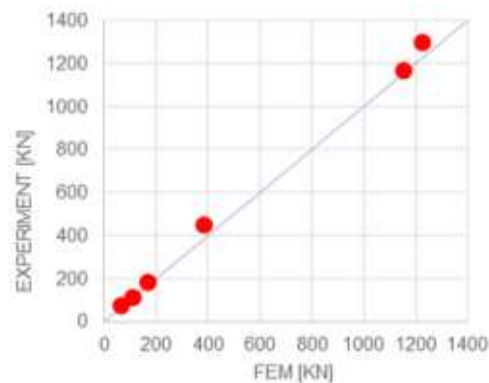
Validation and verification

Componentbased FEM  
Slender plates  
Bolted joints

Connection behaviour  
Open sections  
Hollow sections

Summary

- Validation of research FEM model for resistance



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## Design model of slender plate in compression

Introduction  
Connection design  
Models  
Hollow sections  
Component method  
FE analyse

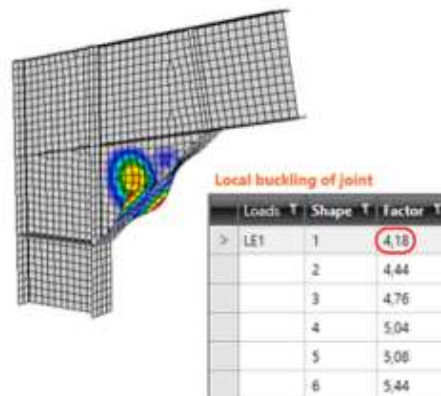
Validation and verification

Componentbased FEM  
Slender plates  
Bolted joints

Connection behaviour  
Open sections  
Hollow sections

Summary

- Buckling analysis



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## Design model of slender plate in compression

Introduction

Connection design

Models

Hollow sections

Component

method

FE analysis

Validation

and verification

Componentbased

FEM

Slender plates

Bolts joints

Connection behaviour

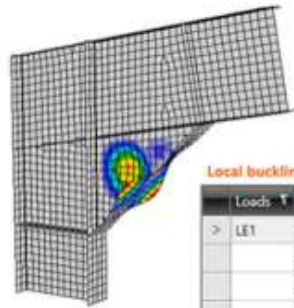
Open sections

Hollow sections

Summary



### • Buckling analysis



Local buckling of joint

Loads	Shape	Factor
> LE1	1	4.18
	2	4.44
	3	4.76
	4	5.04
	5	5.08
	6	5.44



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## Design model of slender plate in compression

Introduction

Connection design

Models

Hollow sections

Component

method

FE analysis

Validation

and verification

Componentbased

FEM

Slender plates

Bolts joints

Connection behaviour

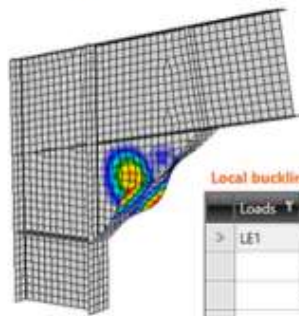
Open sections

Hollow sections

Summary

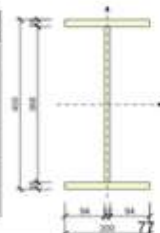


### • Buckling analysis



Local buckling of joint

Loads	Shape	Factor
> LE1	1	4.18
	2	4.44
	3	4.76
	4	5.04
	5	5.08
	6	5.44



## Design model Slender plate in compression

Introduction

Connection design

Models

Hollow sections

Component

method

FE analysis

Validation

and verification

Componentbased

FEM

Slender plates

Bolts joints

Connection behaviour

Open sections

Hollow sections

Summary



To eliminate slender plates in joints

### Reduced stress method

- According to EN 1993-1-5 Annex B
- Critical buckling factor - Linear buckling analyses  $\alpha_{cr}$
- Load amplifier - Material nonlinear analyses  $\alpha_{ult,k}$
- Plate slenderness  $\bar{\lambda}_p = \sqrt{\frac{\sigma_{ult,k}}{\alpha_{cr}}}$
- Plate buckling reduction factor  $\rho$
- Evaluation  $\frac{\rho \cdot \alpha_{ult,k}}{\gamma_{M1}} \geq 1$

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## Design model Slender plate in compression

Introduction

Connection design

Models

Hollow sections

Component

method

FE analyse

Validation  
and verification

Componentbased  
FEM

Slender plates

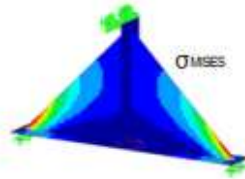
Bolted joints

Connection behaviour

Open sections

Hollow sections

Summary

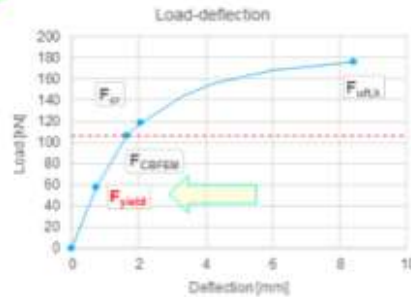


$$\sigma_{MISES} = f_y$$

$$F = 57,6 \text{ kN}$$

$$z = 0,7 \text{ mm}$$

$$\epsilon = 0,25\%$$



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## Design model Slender plate in compression

Introduction

Connection design

Models

Hollow sections

Component

method

FE analyse

Validation  
and verification

Componentbased  
FEM

Slender plates

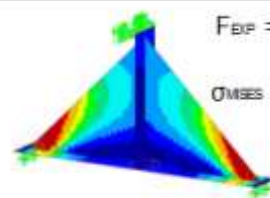
Bolted joints

Connection behaviour

Open sections

Hollow sections

Summary



$$F_{EXP} = 109,7 \text{ kN}$$

$$F = 105,8 \text{ kN}$$

$$z = 1,6 \text{ mm}$$

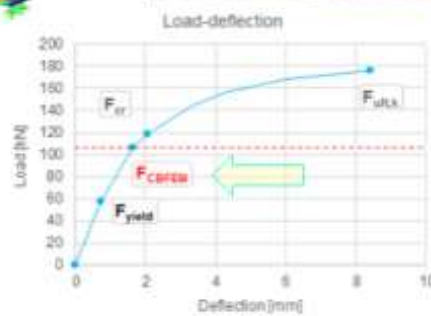
$$\epsilon = 0,7\%$$

$$\alpha_\sigma = 1,123$$

$$\alpha_{ultx} = 1,659$$

$$\rho = 0,603$$

$$1,001 > 1 \text{ OK}$$



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## Design model Slender plate in compression

Introduction

Connection design

Models

Hollow sections

Component

method

FE analyse

Validation  
and verification

Componentbased  
FEM

Slender plates

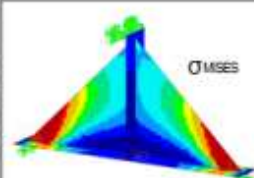
Bolted joints

Connection behaviour

Open sections

Hollow sections

Summary

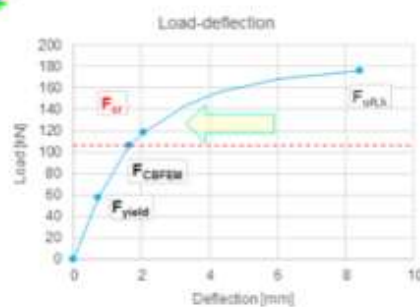


$$F = 118,8 \text{ kN}$$

$$z = 2,1 \text{ mm}$$

$$\epsilon = 1\%$$

$$\alpha_\sigma = 1,0$$

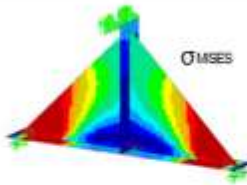


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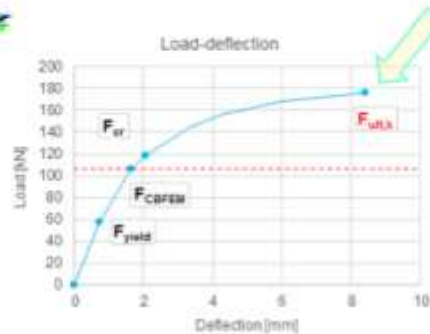


## Design model Slender plate in compression

- Introduction
- Connection design
  - Models
  - Hollow sections
  - Component method
  - FE analyse
- Validation and verification
- Componentbased FEM
  - Slender plates
  - Bolted joints
- Connection behaviour
  - Open sections
  - Hollow sections
- Summary



$F = 175,6 \text{ kN}$   
 $z = 8,4 \text{ mm}$   
 $\epsilon = 5\%$



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## Design model of bolted connections

- Introduction
- Connection design
  - Models
  - Hollow sections
  - Component method
  - FE analyse
- Validation and verification
- Componentbased FEM
  - Slender plates
  - Bolted joints
- Connection behaviour
  - Open sections
  - Hollow sections
- Summary

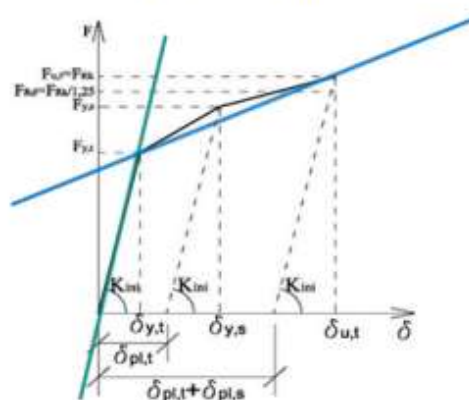
- In shear
- In tension
- Nonpreloaded
  - Are preloaded
- Preloaded bolts
  - Controlled slip

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## Design model of bolt in tension

- Introduction
- Connection design
  - Models
  - Hollow sections
  - Component method
  - FE analyse
- Validation and verification
- Componentbased FEM
  - Slender plates
  - Bolted joints
- Connection behaviour
  - Open sections
  - Hollow sections
- Summary

- Force-displacement diagram



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## Bolted connection

### Deformation stiffness of bolt in tension

Introduction

Connection design

Models

Hollow sections

Component method

FE analyse

Validation and verification

Componentbased FEM

Slender plates

**Bolted joints**

Connection behaviour

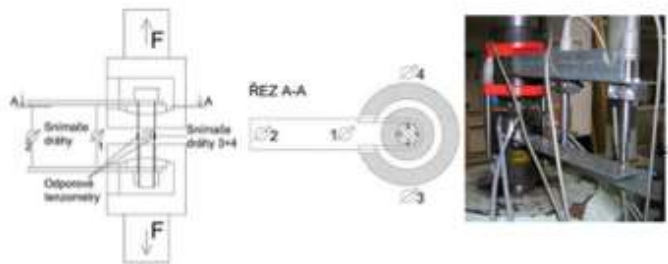
Open sections

Hollow sections

Summary



- References from literature
- Experimental research



## List of own experiments

Introduction

Connection design

Models

Hollow sections

Component method

FE analyse

Validation and verification

Componentbased FEM

Slender plates

**Bolted joints**

Connection behaviour

Open sections

Hollow sections

Summary



- Two failure modes
  - Rupture of thread
  - Tearing down of nut

No.	Concrete	Material	Bolt length [mm]	Orp length [mm]	Nut length [mm]	Flange length [mm]	Head length [mm]
1	M20	8.8	81.5	42.2	15	0	12.6
2	M16	10.9	109	35.4	17	2x4	10.1
3	M16	10.9	108.2	4	17	2x4.1	10.2
4	M16	10.9	108.2	10.5	12.7	2x4.1	10.2
5	M20	8.8	57.7	32.9	15.1	0	12.6
6	M20	8.8	0	99.3	15.6	3.1x3.2	12.6
7	M20	8.8	57.3	34.4	15.5	0	12.5
8	M20	8.8	57.7	32.1	15.2	2x3	12.5
9	M20	8.8	57.7	31.7	15.3	0	12.5
10	M20	8.8	83.4	19.4	30.4	2x2.9	12.7
11	M20	8.8	0	83.5	31	0	12.5
12	M16	10.9	107.7	18.6	17.1	0	10.2
13	M16	10.9	108.1	25.4	12.7	2x4.1	10



## Behaviour based on bolt failure

Introduction

Connection design

Models

Hollow sections

Component method

FE analyse

Validation and verification

Componentbased FEM

Slender plates

**Bolted joints**

Connection behaviour

Open sections

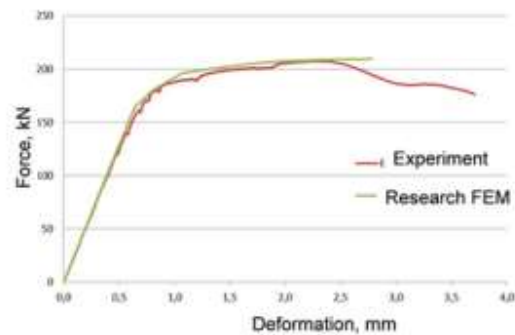
Hollow sections

Summary



## Validation for rupture of thread

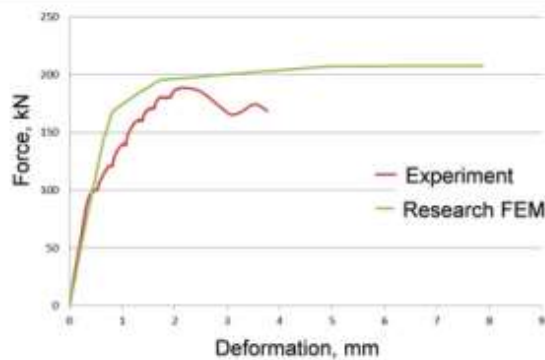
- Introduction
- Connection design
  - Models
  - Hollow sections
  - Component method
  - FE analyse
- Validation and verification
- Componentbased FEM
  - Slender plates
  - Rotated joints**
- Connection behaviour
  - Open sections
  - Hollow sections
- Summary



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## Validation for tearing down of nut

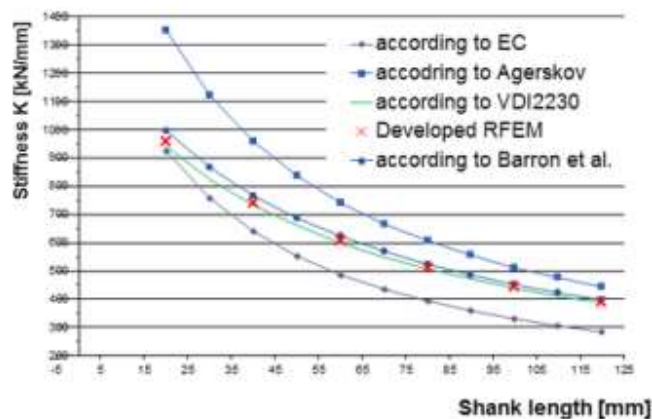
- Introduction
- Connection design
  - Models
  - Hollow sections
  - Component method
  - FE analyse
- Validation and verification
- Componentbased FEM
  - Slender plates
  - Rotated joints**
- Connection behaviour
  - Open sections
  - Hollow sections
- Summary



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## Parametric study of the bolt tensile stiffness

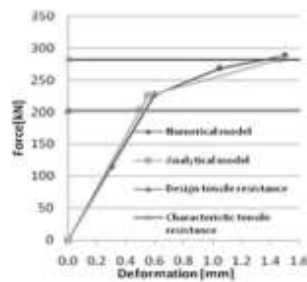
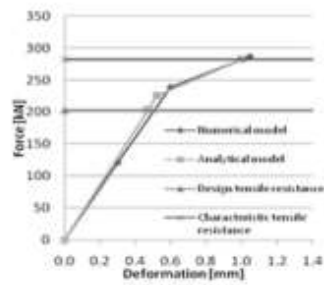
- Introduction
- Connection design
  - Models
  - Hollow sections
  - Component method
  - FE analyse
- Validation and verification
- Componentbased FEM
  - Slender plates
  - Rotated joints**
- Connection behaviour
  - Open sections
  - Hollow sections
- Summary



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## Verification of design model of bolt in tension

- Introduction
- Connection design
  - Models
  - Hollow sections
  - Component method
  - FE analyse
- Validation and verification
- Componentbased FEM
  - Slender plates
  - Bolted joints**
- Connection behaviour
  - Open sections
  - Hollow sections
- Summary



Thread length 17,6 mm      Thread length 28,2 mm

Bolts M24 grade 8.8

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## Modelling of T stub behaviour

- Introduction
- Connection design
  - Models
  - Hollow sections
  - Component method
  - FE analyse
- Validation and verification
- Componentbased FEM
  - Slender plates
  - Bolted joints**
- Connection behaviour
  - Open sections
  - Hollow sections
- Summary

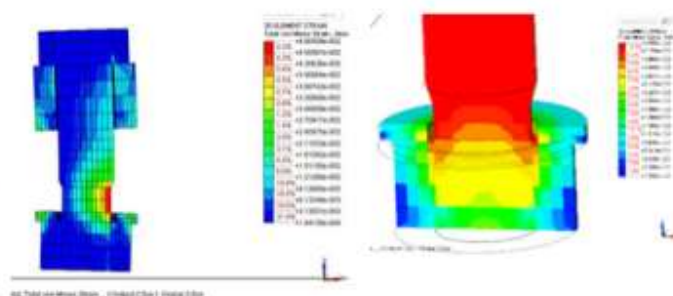
- Research model
  - Validation
- Design model
  - Verification

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## Bolts research model

- Introduction
- Connection design
  - Models
  - Hollow sections
  - Component method
  - FE analyse
- Validation and verification
- Componentbased FEM
  - Slender plates
  - Bolted joints**
- Connection behaviour
  - Open sections
  - Hollow sections
- Summary

- Unequal stresses distribution  
in the threaded part of the bolt



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## T stub behaviour Research FE model

Introduction

Connection design

Models

Hollow sections

Component

method

FE analyse

Validation

and verification

Componentbased

FEM

Slender plates

→ Bolted joints

Connection behaviour

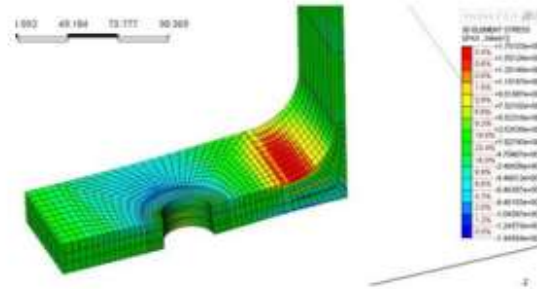
Open sections

Hollow sections

Summary



### • Mesh sensitivity



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## T stub behaviour Research FE model

Introduction

Connection design

Models

Hollow sections

Component

method

FE analyse

Validation

and verification

Componentbased

FEM

Slender plates

→ Bolted joints

Connection behaviour

Open sections

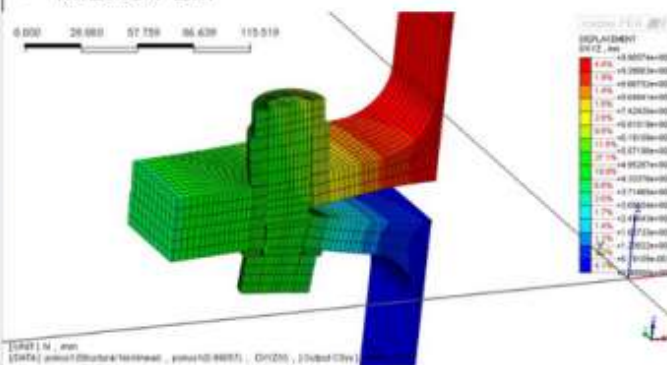
Hollow sections

Summary



### • Bending of bolt

### • MIDAS FEM



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## Experiment with T stub

Introduction

Connection design

Models

Hollow sections

Component

method

FE analyse

Validation

and verification

Componentbased

FEM

Slender plates

→ Bolted joints

Connection behaviour

Open sections

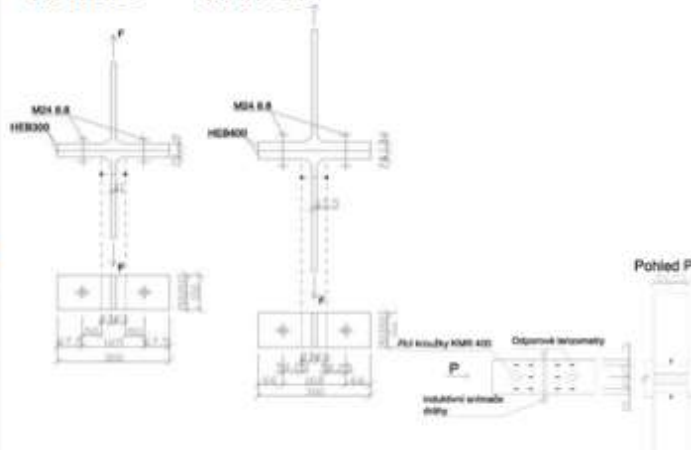
Hollow sections

Summary



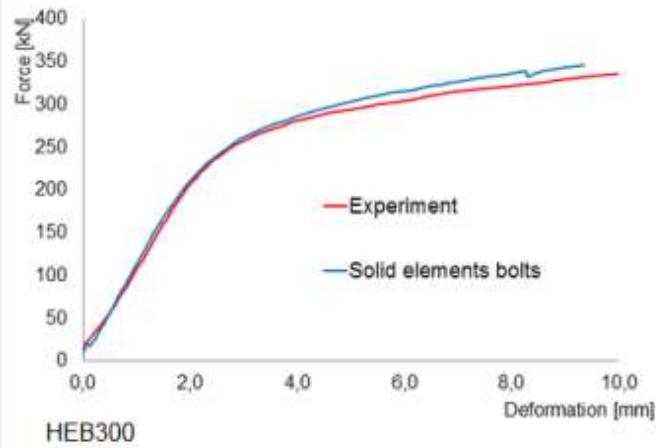
HEB300

HEB400



## Validation – global deformation

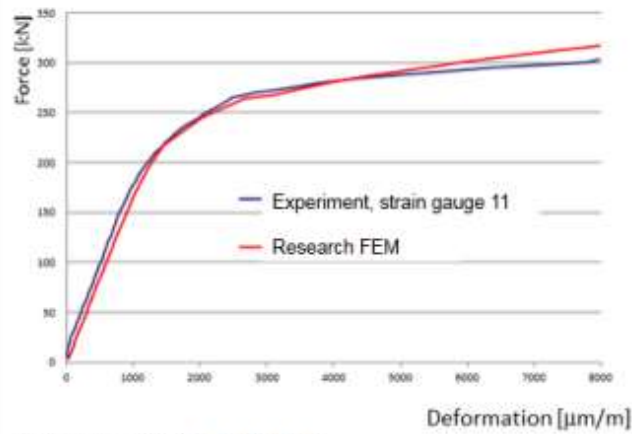
- Introduction
- Connection design
  - Models
  - Hollow sections
  - Component method
  - FE analyse
- Validation and verification
- Componentbased FEM
  - Slender plates
  - Bolts joints**
- Connection behaviour
  - Open sections
  - Hollow sections
- Summary



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## Validation – local deformation

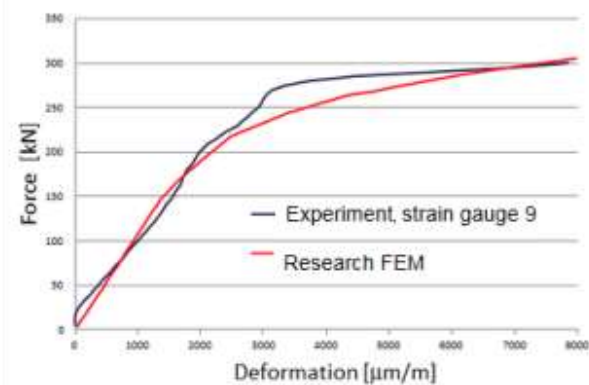
- Introduction
- Connection design
  - Models
  - Hollow sections
  - Component method
  - FE analyse
- Validation and verification
- Componentbased FEM
  - Slender plates
  - Bolts joints**
- Connection behaviour
  - Open sections
  - Hollow sections
- Summary



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## Validation – local deformation

- Introduction
- Connection design
  - Models
  - Hollow sections
  - Component method
  - FE analyse
- Validation and verification
- Componentbased FEM
  - Slender plates
  - Bolts joints**
- Connection behaviour
  - Open sections
  - Hollow sections
- Summary



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# Experiment with T stub

Introduction

Connection design

Models

Hollow sections

Component

method

FE analyse

Validation  
and verification

Componentbased  
FEM

Slender plates

→ Bolted joints

Connection behaviour

Open sections

Hollow sections

Summary



HEB400



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## Validation – global deformation

Introduction

Connection design

Models

Hollow sections

Component

method

FE analyse

Validation  
and verification

Componentbased  
FEM

Slender plates

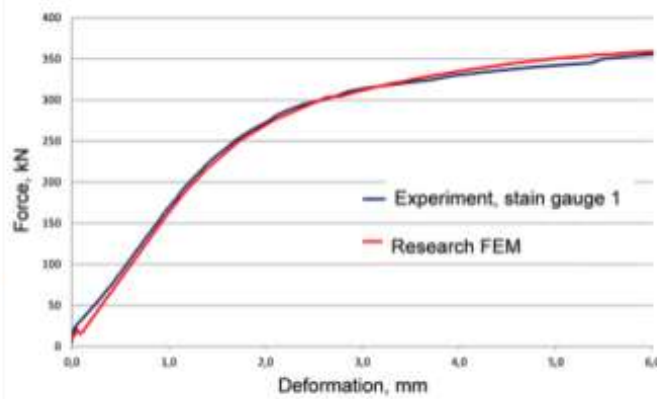
→ Bolted joints

Connection behaviour

Open sections

Hollow sections

Summary



HEB 400

## T stub design model Verification

Introduction

Connection design

Models

Hollow sections

Component

method

FE analyse

Validation  
and verification

Componentbased  
FEM

Slender plates

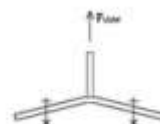
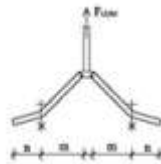
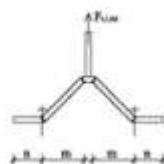
→ Bolted joints

Connection behaviour

Open sections

Hollow sections

Summary



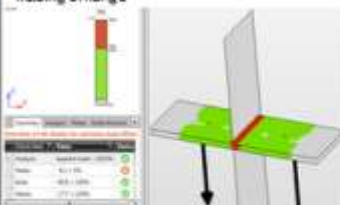
$$F_{t1,Bd} = \frac{(8n - 2\theta_w) M_{pl1} R_d}{2(m + \theta_w)(m + n)}$$

$$F_{t2,Bd} = \frac{2M_{pl2} R_d + 2n F_{t1,Bd}}{m + n}$$

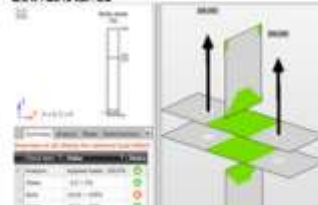
$$F_{t3,Bd} = 2F_{t1,Bd}$$

CBFEM:

Yielding of flange



Bolt resistance



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## T stub design model Verification

Introduction

Connection design

Models

Hollow sections

Component

method

FE analyse

Validation

and verification

Componentbased

FEM

Slender plates

Noted joints

Connection behaviour

Open sections

Hollow sections

Summary



Flange thickness $t_f$	Component method		CBFEM		3D FEM	
	Resistance [kN]	Failure	Resistance [kN]	Failure	Resistance [kN]	Failure
10	44	1	75	1	115	1
12	63	1	90	1	144	1
15	98	1	115	1	199.7	1
20	174	1	175	1	268.8	2
25	279	2	249	1	310.3	2
30	305	2	288	2	328.7	2
35	335	2	320	2	347.3	2
40	371	2	358	2	370.7	2
45	407	3	385	2	400	2
50	407	3	412	3	407	3

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## T stub design model Verification

Introduction

Connection design

Models

Hollow sections

Component

method

FE analyse

Validation

and verification

Componentbased

FEM

Slender plates

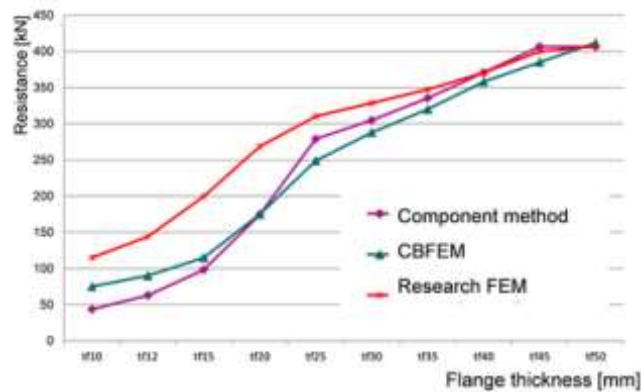
Noted joints

Connection behaviour

Open sections

Hollow sections

Summary



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## T stub design model Verification

Introduction

Connection design

Models

Hollow sections

Component

method

FE analyse

Validation

and verification

Componentbased

FEM

Slender plates

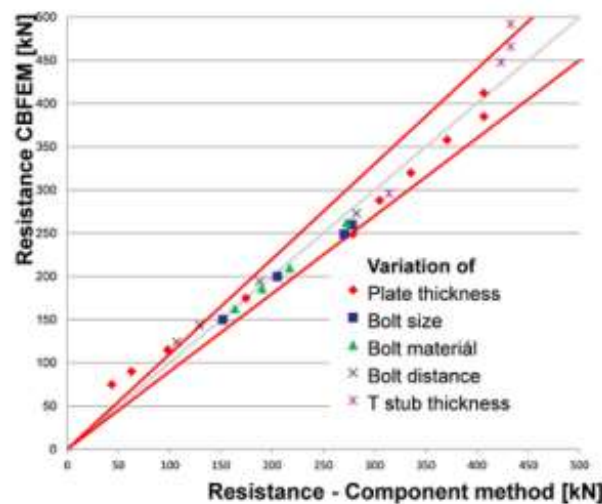
Noted joints

Connection behaviour

Open sections

Hollow sections

Summary



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## Connection behaviour bolted connections of open section

- Introduction
- Connection design
  - Models
  - Hollow sections
  - Component method
  - FE analyse
- Validation and verification
- Componentbased FEM
  - Slender plates
  - Bolted joints
- Connection behaviour
  - Open sections
  - Hollow sections
- Summary



- Generally
  - Shear
  - Tension
  - Compression
- Research model
  - Validation
- Design model
  - Verification

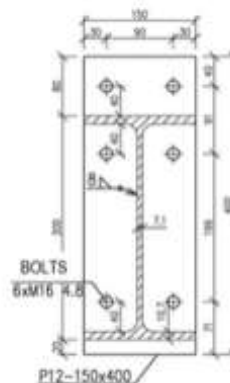
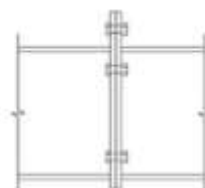
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## Verification bolts in tension and in shear

- Introduction
- Connection design
  - Models
  - Hollow sections
  - Component method
  - FE analyse
- Validation and verification
- Componentbased FEM
  - Slender plates
  - Bolted joints
- Connection behaviour
  - Open sections
  - Hollow sections
- Summary



### Beam splices joint



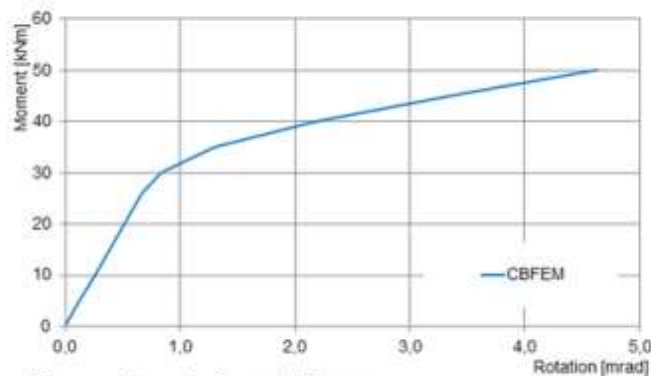
### End plate connection

Steel S355  
Plate 12 mm  
Bolts M16 4.8

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## Verification bolts in tension and in shear

- Introduction
- Connection design
  - Models
  - Hollow sections
  - Component method
  - FE analyse
- Validation and verification
- Componentbased FEM
  - Slender plates
  - Bolted joints
- Connection behaviour
  - Open sections
  - Hollow sections
- Summary

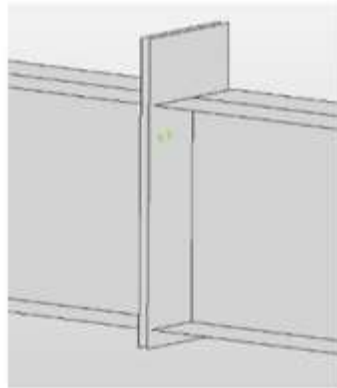


Moment - rotational diagram  
predicted by CBFEM and CM

110

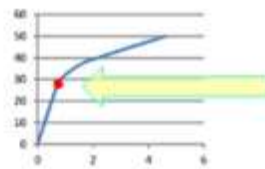
## Global behaviour bolts in tension and in shear

- Introduction
- Connection design
  - Models
  - Hollow sections
  - Component method
  - FE analyse
- Validation and verification
- Componentbased FEM
  - Slender plates
  - Bolled joints
- Connection behaviour
  - Open sections
  - Hollow sections
- Summary



$M=28 \text{ kNm}$   
 $F_i=0,746 \text{ mrad}$   
 $S_i=37,5 \text{ MNm/rad}$

Moment, kNm



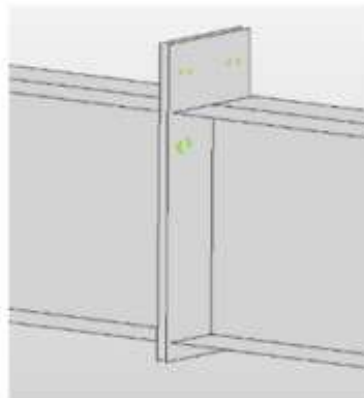
Rotation, mrad

Elastic stresses

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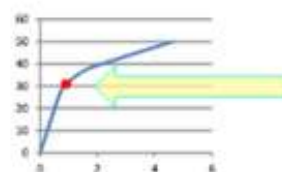
## Global behaviour bolts in tension and in shear

- Introduction
- Connection design
  - Models
  - Hollow sections
  - Component method
  - FE analyse
- Validation and verification
- Componentbased FEM
  - Slender plates
  - Bolled joints
- Connection behaviour
  - Open sections
  - Hollow sections
- Summary



$M=31 \text{ kNm}$   
 $F_i=0,898 \text{ mrad}$   
 $S_i=34,5 \text{ MNm/rad}$

Moment, kNm



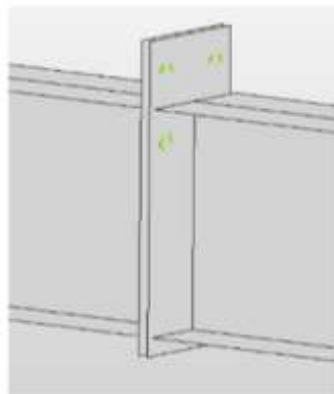
Rotation, mrad

Plastification round the lower bolts

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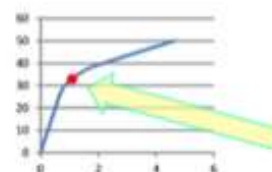
## Global behaviour bolts in tension and in shear

- Introduction
- Connection design
  - Models
  - Hollow sections
  - Component method
  - FE analyse
- Validation and verification
- Componentbased FEM
  - Slender plates
  - Bolled joints
- Connection behaviour
  - Open sections
  - Hollow sections
- Summary



$M=33 \text{ kNm}$   
 $F_i=1,089 \text{ mrad}$   
 $S_i=30,3 \text{ MNm/rad}$

Moment, kNm



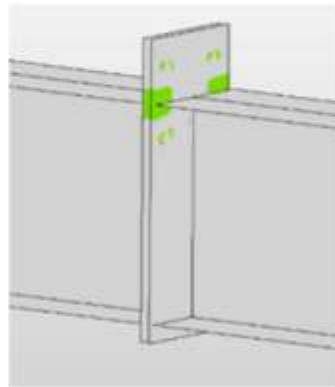
Rotation, mrad

Plastification round the upper bolts

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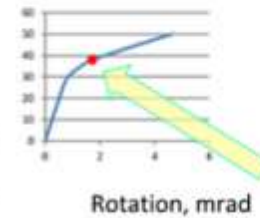
## Global behaviour bolts in tension and in shear

- Introduction
- Connection design
  - Models
  - Hollow sections
  - Component method
  - FE analyse
- Validation and verification
- Componentbased FEM
  - Slender plates
  - Bolted joints
- Connection behaviour
  - Open sections
  - Hollow sections
- Summary



$M=38 \text{ kNm}$   
 $F_i=1,714 \text{ mrad}$   
 $S_i=22,2 \text{ MNm/rad}$

Moment, kNm



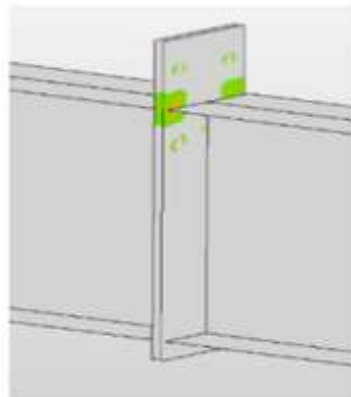
Rotation, mrad

Plastification round the flanges

114

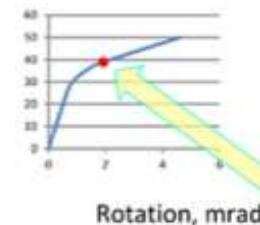
## Global behaviour bolts in tension and in shear

- Introduction
- Connection design
  - Models
  - Hollow sections
  - Component method
  - FE analyse
- Validation and verification
- Componentbased FEM
  - Slender plates
  - Bolted joints
- Connection behaviour
  - Open sections
  - Hollow sections
- Summary



$M=39 \text{ kNm}$   
 $F_i=1,925 \text{ mrad}$   
 $S_i=20,3 \text{ MNm/rad}$

Moment, kNm



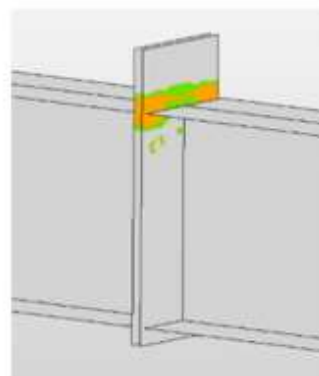
Rotation, mrad

Plastification in the web of HEA

115

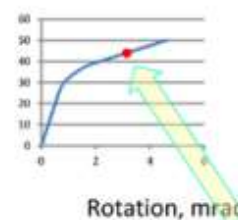
## Global behaviour bolts in tension and in shear

- Introduction
- Connection design
  - Models
  - Hollow sections
  - Component method
  - FE analyse
- Validation and verification
- Componentbased FEM
  - Slender plates
  - Bolted joints
- Connection behaviour
  - Open sections
  - Hollow sections
- Summary



$M=44 \text{ kNm}$   
 $F_i=3,138 \text{ mrad}$   
 $S_i=14,0 \text{ MNm/rad}$

Moment, kNm



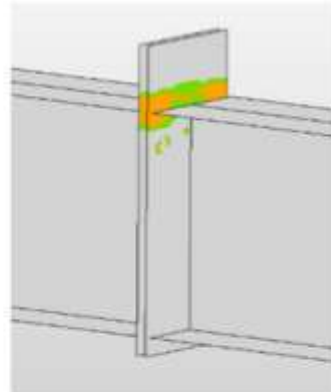
Rotation, mrad

Plastification in the web of HEA

116

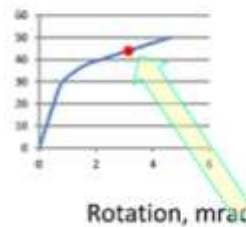
## Global behaviour bolts in tension and in shear

- Introduction
- Connection design
  - Models
  - Hollow sections
  - Component method
  - FE analyse
- Validation and verification
- Componentbased FEM
  - Slender plates
  - Bolted joints
- Connection behaviour
  - Open sections
  - Hollow sections
- Summary



$M=44 \text{ kNm}$   
 $F_i=3,138 \text{ mrad}$   
 $S_i=14,0 \text{ MNm/rad}$

Moment, kNm

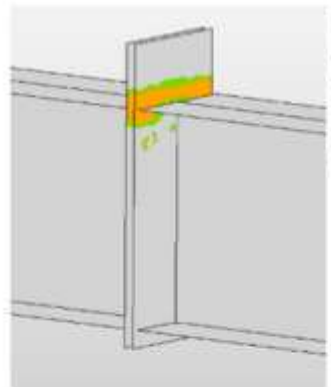


Rotation, mrad

Plastification in the web of HEA

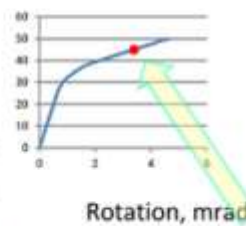
## Global behaviour bolts in tension and in shear

- Introduction
- Connection design
  - Models
  - Hollow sections
  - Component method
  - FE analyse
- Validation and verification
- Componentbased FEM
  - Slender plates
  - Bolted joints
- Connection behaviour
  - Open sections
  - Hollow sections
- Summary



$M=45 \text{ kNm}$   
 $F_i=3,383 \text{ mrad}$   
 $S_i=13,3 \text{ MNm/rad}$

Moment, kNm



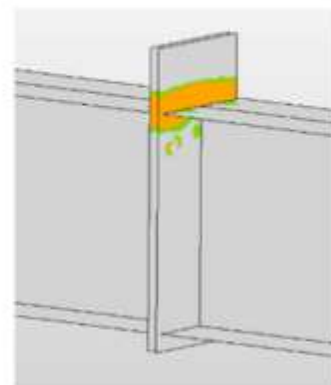
Rotation, mrad

Plastification in the web of HEA

118

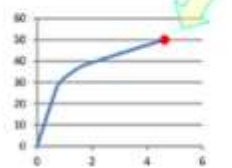
## Global behaviour bolts in tension and in shear

- Introduction
- Connection design
  - Models
  - Hollow sections
  - Component method
  - FE analyse
- Validation and verification
- Componentbased FEM
  - Slender plates
  - Bolted joints
- Connection behaviour
  - Open sections
  - Hollow sections
- Summary



$M=50 \text{ kNm}$   
 $F_i=4,626 \text{ mrad}$   
 $S_i=10,8 \text{ MNm/rad}$

Moment, kNm



Rotation, mrad

Full plastification in the web of HEA

119



## Verification bolts in tension

Introduction

Connection design

Models

Hollow sections

Component method

FE analyse

Validation and verification

Componentbased FEM

Slender plates

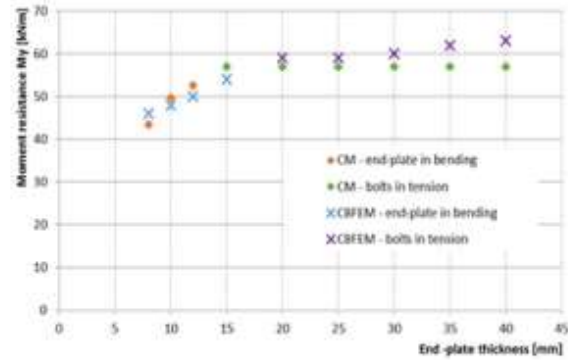
Bolted joints

Connection behaviour

Open sections

Hollow sections

Summary



End plate thickness

120

## Verification bolts in tension

Introduction

Connection design

Models

Hollow sections

Component method

FE analyse

Validation and verification

Componentbased FEM

Slender plates

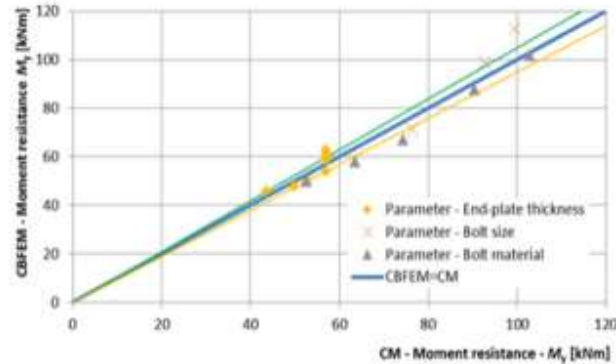
Bolted joints

Connection behaviour

Open sections

Hollow sections

Summary



Geometrical and material parameter

121

## Verification bolts in shear

Introduction

Connection design

Models

Hollow sections

Component method

FE analyse

Validation and verification

Componentbased FEM

Slender plates

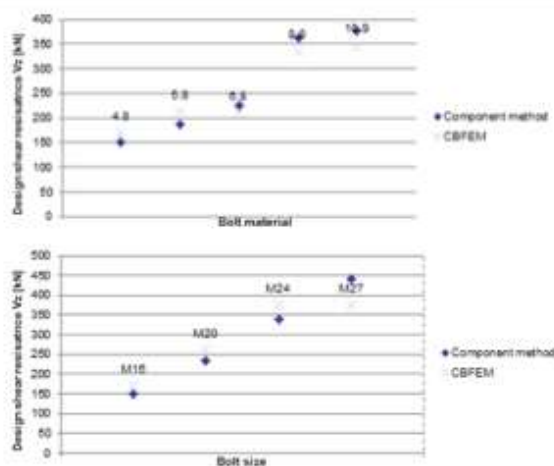
Bolted joints

Connection behaviour

Open sections

Hollow sections

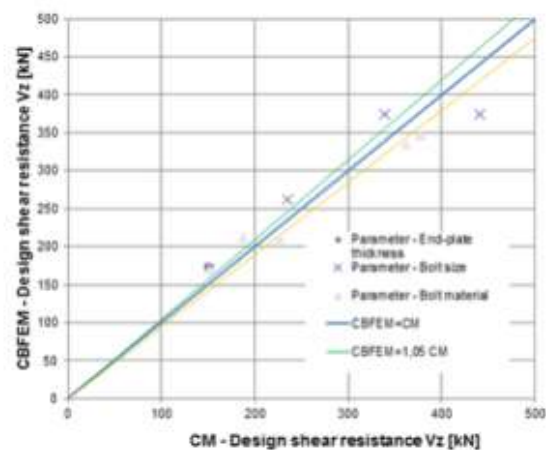
Summary



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## Verification bolts in shear

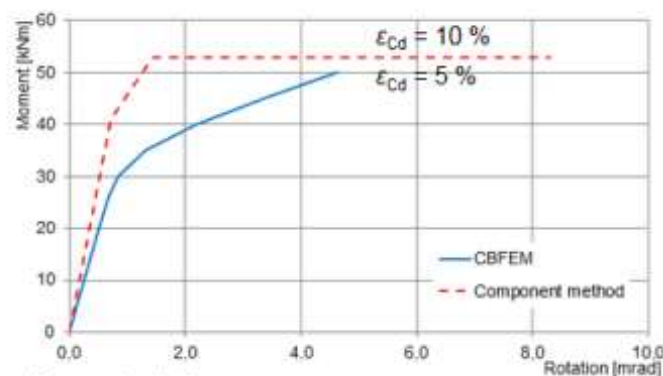
- Introduction
- Connection design
  - Models
  - Hollow sections
  - Component method
  - FE analyse
- Validation and verification
- Componentbased FEM
  - Slender plates
  - Bolts joints
- Connection behaviour
  - Open sections
  - Hollow sections
- Summary



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## Verification deformation capacity

- Introduction
- Connection design
  - Models
  - Hollow sections
  - Component method
  - FE analyse
- Validation and verification
- Componentbased FEM
  - Slender plates
  - Bolts joints
- Connection behaviour
  - Open sections
  - Hollow sections
- Summary



Component method by  
Beg D., Zupan Đ. E., Vayas I., On the rotation capacity of moment connections,  
*Journal of Constructional Steel Research* 60, 3–5, 2004, 601–620.

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## Prediction of Deformation capacity

- Introduction
- Connection design
  - Models
  - Hollow sections
  - Component method
  - FE analyse
- Validation and verification
- Componentbased FEM
  - Slender plates
  - Bolts joints
- Connection behaviour
  - Open sections
  - Hollow sections
- Summary

- Material
  - For resistance  $\epsilon_{Cd} = 5 \%$
  - For deformation capacity  $\epsilon_{Cd} = 15 \%$

- Actual yield strength  
EN 1998-1-8 cl. 6.2  
Overstrenght factor  $g_{ov} = 1,25$

$$f_{y,max} \leq 1,1 g_{ov} f_y$$



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# Generally loaded connections

## Experiments – beam splices

**Introduction**

**Connection design**

- Models
- Hollow sections
- Component method
- FE analyse

**Validation and verification**


**Componentbased FEM**

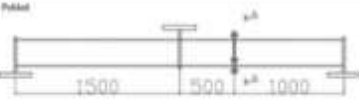


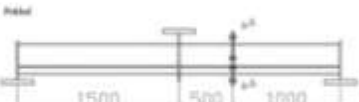





- Slender plates
- Bolted joints

**Connection behaviour**

- Open sections
- Hollow sections

**Summary**



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# Verification to component model

## Welded portal frame eaves moment connection

**Introduction**

**Connection design**

- Models
- Hollow sections
- Component method
- FE analyse

**Validation and verification**


**Componentbased FEM**

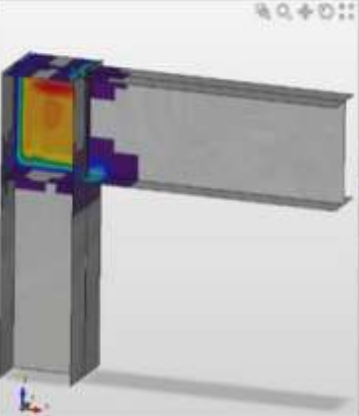

- Slender plates
- Bolted joints

**Connection behaviour**

- Open sections
- Hollow sections

**Summary**



Beam IPE330 to column HEB260 connection

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# Verification to component model

## Welded portal frame eaves moment connection

**Introduction**

**Connection design**

- Models
- Hollow sections
- Component method
- FE analyse

**Validation and verification**


**Componentbased FEM**

- Slender plates
- Bolted joints

**Connection behaviour**

- Open sections
- Hollow sections

**Summary**

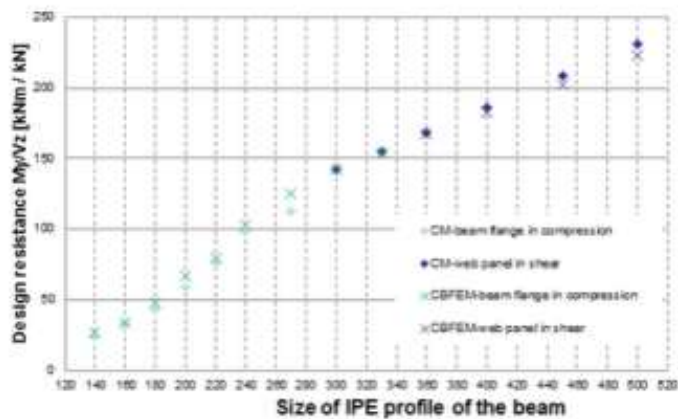


Parameter	Component method		CBFEM-idea RS	
	Resistance [kN/kNm]	Critical component	Resistance [kN/kNm]	Critical component
IPE140	24	Beam flange in compression	27	Beam flange in compression
IPE160	33	Beam flange in compression	34	Beam flange in compression
IPE180	44	Beam flange in compression	48	Beam flange in compression
IPE200	59	Beam flange in compression	67	Beam flange in compression
IPE220	77	Beam flange in compression	80	Beam flange in compression
IPE240	98	Beam flange in compression	103	Beam flange in compression
IPE270	113	Beam flange in compression	125	Beam flange in compression
IPE300	142	Web panel in shear	142	Beam flange in compression
IPE320	155	Web panel in shear	154	Beam flange in compression
IPE360	168	Web panel in shear	167	Web panel in shear
IPE400	186	Web panel in shear	183	Web panel in shear
IPE450	209	Web panel in shear	202	Web panel in shear
IPE500	231	Web panel in shear	223	Web panel in shear

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## Verification to component model Welded portal frame eaves moment connection

- Introduction
- Connection design
  - Models
  - Hollow sections
  - Component method
  - FE analyse
- Validation and verification
- Componentbased FEM
  - Slender plates
  - Bolted joints
- Connection behaviour
  - Open sections
  - Hollow sections
- Summary



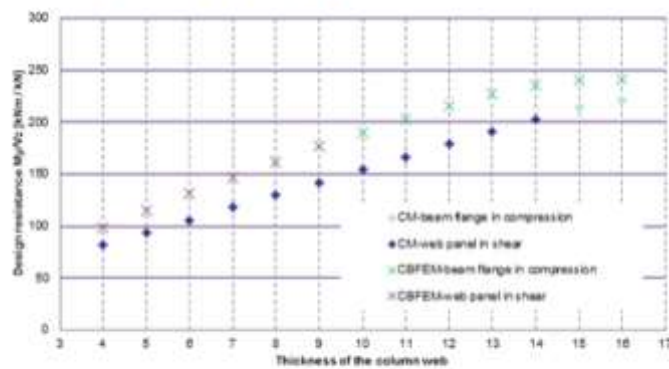
129

## Verification to component model Welded portal frame eaves moment connection

- Introduction
- Connection design
  - Models
  - Hollow sections
  - Component method
  - FE analyse
- Validation and verification
- Componentbased FEM
  - Slender plates
  - Bolted joints
- Connection behaviour
  - Open sections
  - Hollow sections
- Summary



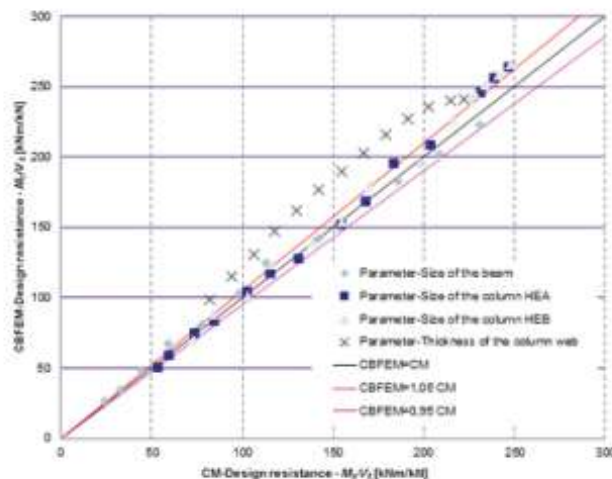
○ Thickness of the column web



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## Verification to component model Welded portal frame eaves moment connection

- Introduction
- Connection design
  - Models
  - Hollow sections
  - Component method
  - FE analyse
- Validation and verification
- Componentbased FEM
  - Slender plates
  - Bolted joints
- Connection behaviour
  - Open sections
  - Hollow sections
- Summary



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## Joint between open and hollow section

- Introduction
- Connection design
  - Models
  - Hollow sections
  - Component method
  - FE analyse
- Validation and verification
- Componentbased FEM
  - Slender plates
  - Bolted joints
- Connection behaviour
  - Open sections
  - Hollow sections
- Summary

- Verification
  - Welds
  - FEM meshing



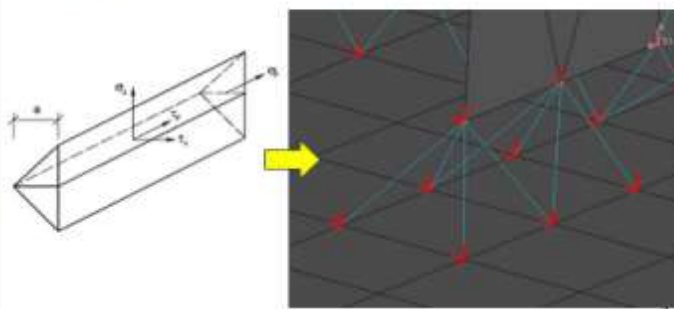
- Benchmark case
  - HEA 240 and hollow section RHS 180x100x10
  - Loaded by bending moment and shear force

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## Welds for FEM design model

- Introduction
- Connection design
  - Models
  - Hollow sections
  - Component method
  - FE analyse
- Validation and verification
- Componentbased FEM
  - Slender plates
  - Bolted joints
- Connection behaviour
  - Open sections
  - Hollow sections
- Summary

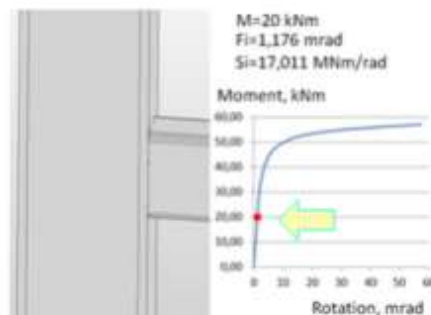
- Model of weld
  - - stiffness, resistance, deformation capacity
  - - stiffness, resistance, deformation capacity
  - - neglected



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## Joint between open and hollow section

- Introduction
- Connection design
  - Models
  - Hollow sections
  - Component method
  - FE analyse
- Validation and verification
- Componentbased FEM
  - Slender plates
  - Bolted joints
- Connection behaviour
  - Open sections
  - Hollow sections
- Summary



Elastic stage

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## Joint between open and hollow section

Introduction

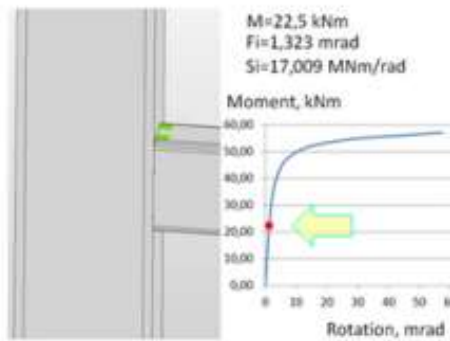
Connection design  
Models  
Hollow sections  
Component method  
FE analyse

Validation and verification

Componentbased FEM  
Slender plates  
Bolted joints

Connection behaviour  
Open sections  
Hollow sections

Summary



Plastification  
of the hollow section RHS upper flange

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## Joint between open and hollow section

Introduction

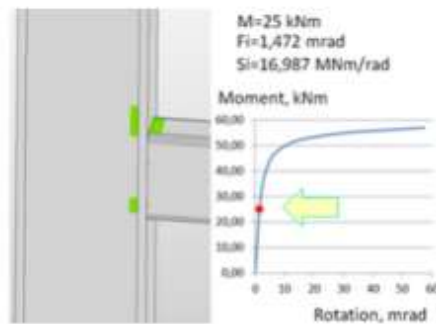
Connection design  
Models  
Hollow sections  
Component method  
FE analyse

Validation and verification

Componentbased FEM  
Slender plates  
Bolted joints

Connection behaviour  
Open sections  
Hollow sections

Summary



Initial plastification  
in the open section web

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## Joint between open and hollow section

Introduction

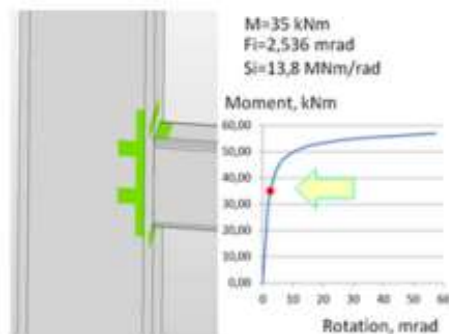
Connection design  
Models  
Hollow sections  
Component method  
FE analyse

Validation and verification

Componentbased FEM  
Slender plates  
Bolted joints

Connection behaviour  
Open sections  
Hollow sections

Summary



Initial plastification  
in the open section flange

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## Joint between open and hollow section

Introduction

Connection design

Models

Hollow sections

Component

method

FE analyse

Validation  
and verification

Componentbased

FEM

Slender plates

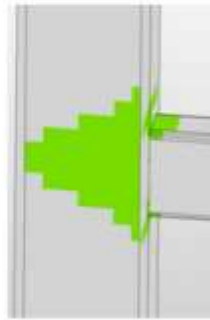
Bolted joints

Connection behaviour

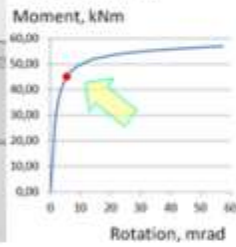
Open sections

Hollow sections

Summary



$M=45 \text{ kNm}$   
 $F_i=5,431 \text{ mrad}$   
 $S_i=8,3 \text{ MNm/rad}$



Full plastification  
through the open section web

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## Joint between open and hollow section

Introduction

Connection design

Models

Hollow sections

Component

method

FE analyse

Validation  
and verification

Componentbased

FEM

Slender plates

Bolted joints

Connection behaviour

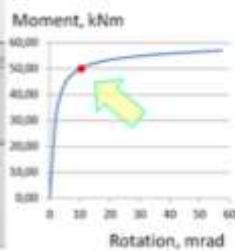
Open sections

Hollow sections

Summary



$M=50 \text{ kNm}$   
 $F_i=10,413 \text{ mrad}$   
 $S_i=4,8 \text{ MNm/rad}$



Initial plastification  
in the hollow section RHS web

## Joint between open and hollow section

Introduction

Connection design

Models

Hollow sections

Component

method

FE analyse

Validation  
and verification

Componentbased

FEM

Slender plates

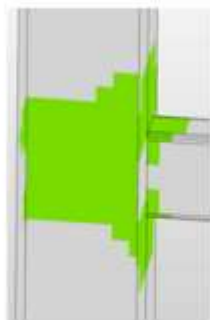
Bolted joints

Connection behaviour

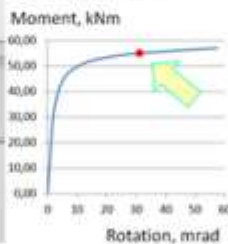
Open sections

Hollow sections

Summary



$M=55 \text{ kNm}$   
 $F_i=31,033 \text{ mrad}$   
 $S_i=1,8 \text{ MNm/rad}$



Plastification  
of second flange of open section HEA

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## Joint between open and hollow section

Introduction

Connection design

Models

Hollow sections

Component

method

FE analyse

Validation

and verification

Componentbased

FEM

Slender plates

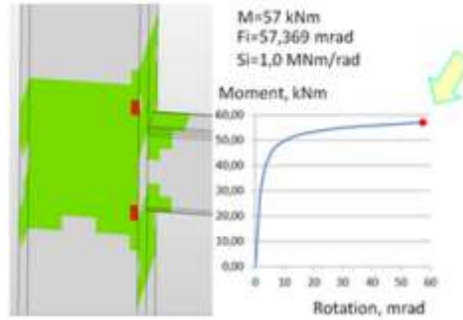
Bolled joints

Connection behaviour

Open sections

Hollow sections

Summary



The open section web reaches design strain 5%

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## Joint between open and hollow section

Introduction

Connection design

Models

Hollow sections

Component

method

FE analyse

Validation

and verification

Componentbased

FEM

Slender plates

Bolled joints

Connection behaviour

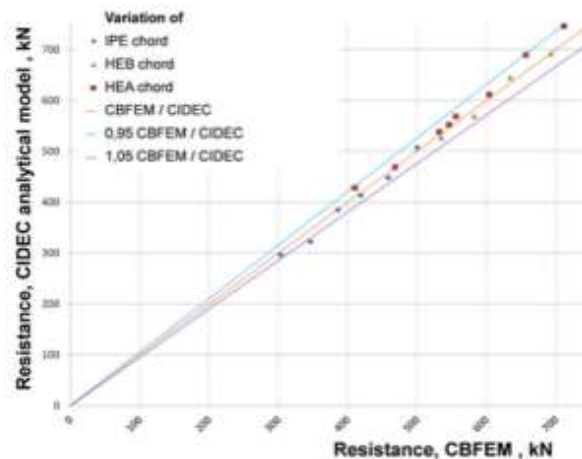
Open sections

Hollow sections

Summary



Verification of resistance CBFEM to CIDEC model



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## Summary

Introduction

Connection design

Models

Hollow sections

Component

method

FE analyse

Validation

and verification

Componentbased

FEM

Slender plates

Bolled joints

Connection behaviour

Open sections

Hollow sections

Summary



- Results shows the good accuracy of CBFEM verified to CM
- For higher stiffness / resistance / deformation capacity CBFEM compare to CM verification by research FEM validated to experiments

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## Summary

Introduction

Connection design  
Models  
Hollow sections  
Component  
method  
FE analyse

Validation  
and verification

Componentbased  
FEM  
Slender plates  
Bolted joints

Connection behaviour  
Open sections  
Hollow sections



**„Verification  
deals with mathematics;  
validation  
deals with physics’**

Roache P.J. (1998) Verification and validation in computational science and engineering, Hermosa Publishers Albuquerque, NM.

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## Summary

Introduction

Connection design  
Models  
Hollow sections  
Component  
method  
FE analyse

Validation  
and verification

Componentbased  
FEM  
Slender plates  
Bolted joints

Connection behaviour  
Open sections  
Hollow sections



- CM in tables and tools limits poor design  
by **incompetent amateurs**
- CBFEM allows properly analysed/checked
  - Complex design solutions
  - Complicatedly loaded joints
  - By **well-trained experts**

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## Summary

Introduction

Connection design  
Models  
Hollow sections  
Component  
method  
FE analyse

Validation  
and verification

Componentbased  
FEM  
Slender plates  
Bolted joints

Connection behaviour  
Open sections  
Hollow sections



- Benchmark cases  
and correct use of V&V  
limits the improper use of model
- The high-quality education  
the background  
of design of pretty structural connections

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## Hierarchy of benchmark studies for structural steel joints

Introduction
Connection design
Models
Hollow sections
Component method
FE analyse
Validation and verification
Component based FEM
Slender plates
Bolts joints
Connection behaviour
Open sections
Hollow sections
Summary

- **Welded joints**
  - In shear
  - In bending
  - Long joint
  - Flexible plate
- **Bolted connections**
  - **T-stub in tension**
  - Splices in shear
  - Generally loaded end plate
- **Slender plate in compression**
  - **Triangular haunch**
  - Stiffener of column web
  - Plate in compression between bolts
- **Hollow section joints**
  - CHS, RHS members
  - Hollow and open sections
- **Column bases**
  - T stub in compression and in tension
  - Generally loaded base plate

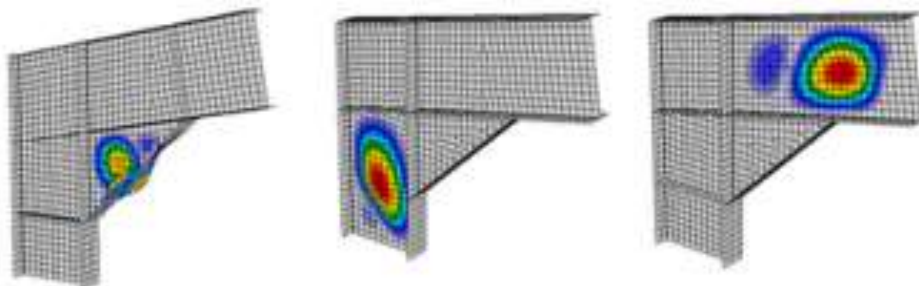
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## Background references Component based FEM

Introduction
Connection design
Models
Hollow sections
Component method
FE analyse
Validation and verification
Component based FEM
Slender plates
Bolts joints
Connection behaviour
Open sections
Hollow sections
Summary

- Wald, F., Gödrich, L., Šabatka L., Kabeláč, J., Navrátil, J., **Component Based Finite Element Model of Structural Connections**. In *Steel, Space and Composite Structures*. Singapore, 2014, 337-344, ISBN 978-981-09-0077-9.
- Gödrich L., Wald F., Sokol Z., **Advanced Modelling of End Plate**. In *Eurosteel 2014*. Brussels, ECCS, 2014, 287-288, ISBN 978-92-9147-121-8.
- Gödrich L., Kurejková M., Wald F., Sokol, Z., **The Bolts and Compressed Plates Modelling**. In *Steel, Space and Composite Structures*, Singapore, 2014, 215-224, ISBN 978-981-09-0077-9.
- Wald F., Šabatka L., Kabeláč J., Kolaja D., Pospíšil M., **Structural Analysis and Design of Steel Connections using Component Based Finite Element Model (CBFEM)**, *Journal of Civil Engineering and Architecture*, 10/2015.

URL: [www.ocel-drevo.fsv.cvut.cz](http://www.ocel-drevo.fsv.cvut.cz)



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